

# Crystal Growth: Physics, Technology and Modeling

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## Lecture 1. Epitaxy - introduction

**22 February 2023**

<http://w3.unipress.waw.pl/~stach/cg-2022-23/>

# Epitaxy - introduction

## Outline

- **definitions**
- **methods of epitaxial growth**
- **lattice mismatch**
- **thermal strain**
- **antiphase domains (polar on non-polar growth)**
- **some methods to reduce defect density in lattice mismatched epitaxial structures**

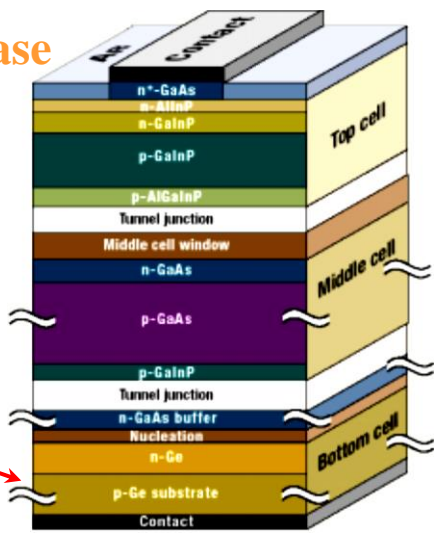


### bulk crystals

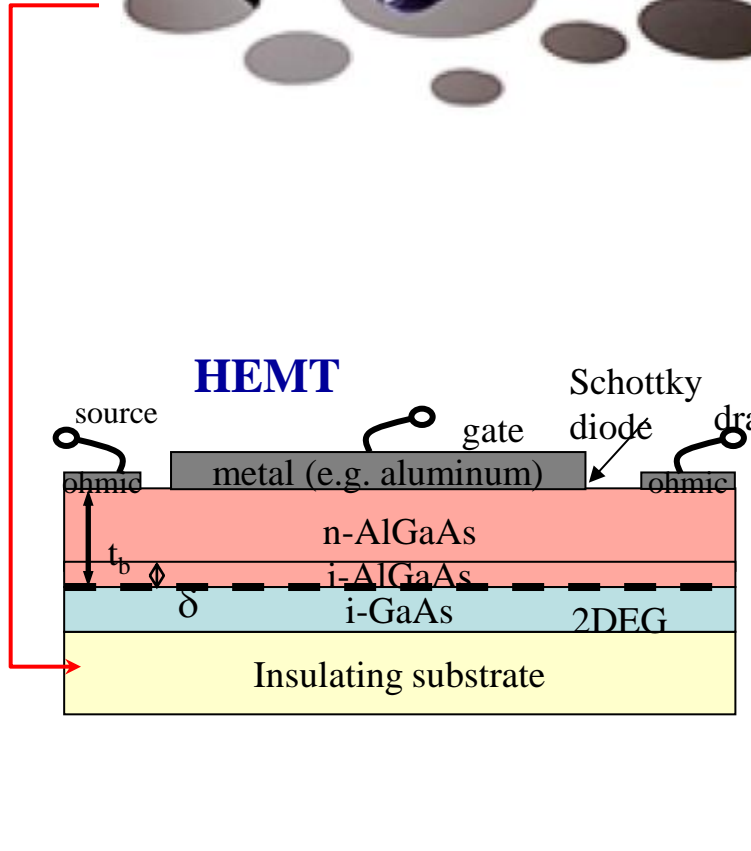
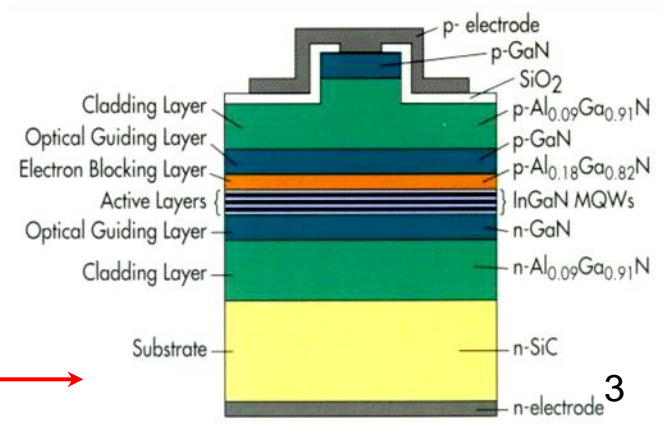
- melt grown
- solution grown
- grown from a gas phase
- .....

### epitaxial structures

### solar cell



### laser diode



~ a few  $\mu\text{m}$

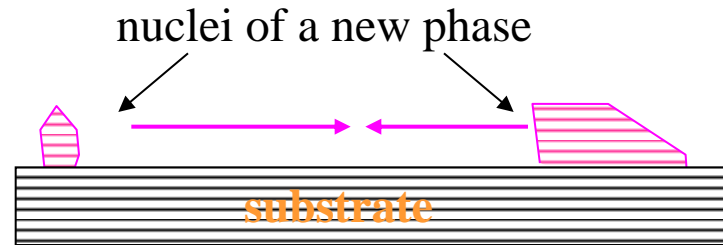
~300  $\mu\text{m}$

# Definitions

- **Epitaxy** = growth of monocrystalline layers on the monocrystalline substrate in the way that crystalline structure of the layer is determined by the structure of the substrate

*epi* = on (above)

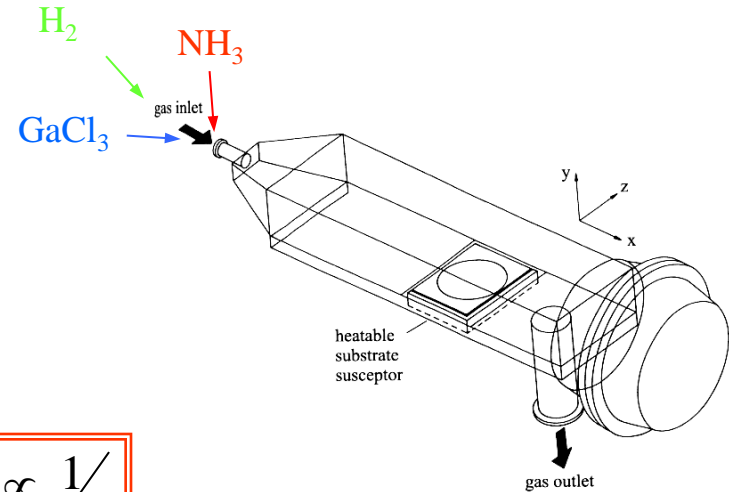
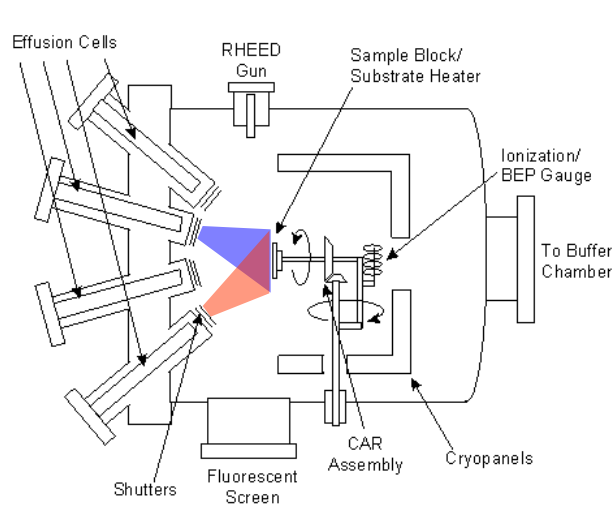
*taxis* = an ordered manner



- **Homoepitaxy** = the layer and the substrate are the same
- **Heteroepitaxy** = the layer and the substrate are different (e.g. they differ by chemical composition)

# Methods of epitaxial growth

- Epitaxy from a gas phase (MBE, VPE, MOVPE, HVPE, ...)  $V_{gr} \sim \mu\text{m/h}$   
 next lectures: Z.R. Żytkiewicz i M. Leszczyński



$$\lambda_{swobodna} \propto \frac{1}{p}$$

non-equilibrium methods

*in situ* growth analysis possible

- Liquid phase epitaxy (LPE, LPEE, ...)  $V_{gr} \sim \mu\text{m/min}$   
 lecture: Z.R. Żytkiewicz 5 April 2023

# Solid Phase Epitaxy

## mass transport mechanism – solid state diffusion

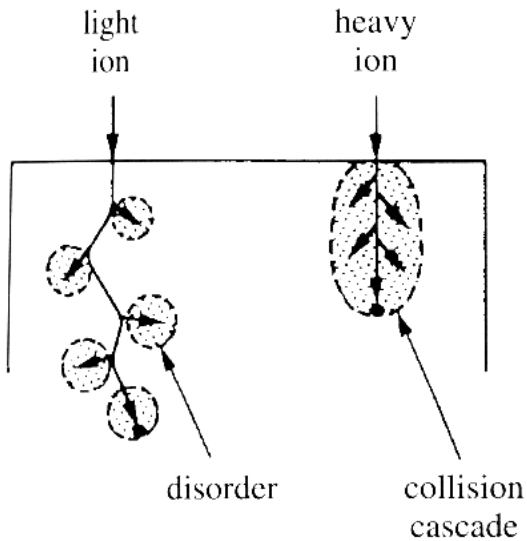
### Examples:

post implantation annealing

low-temperature buffer AlN (GaN)  
(2-step growth)

GaN growth w/o the buffer  
 $T \sim 1000^\circ\text{C}$

AlN nucleation  
 $T \sim 600^\circ\text{C}$



atoms on the surface are mobile

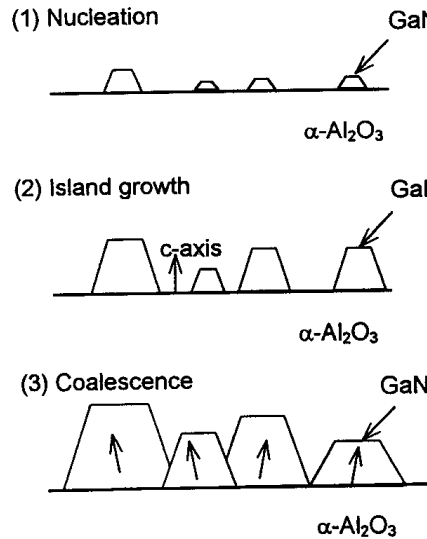


Figure 9. Schematic diagrams of the growth process of GaN on sapphire without an AlN buffer layer.

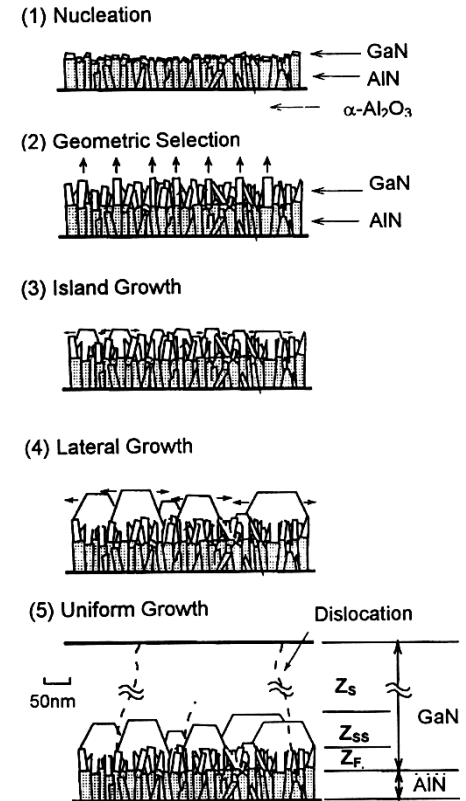
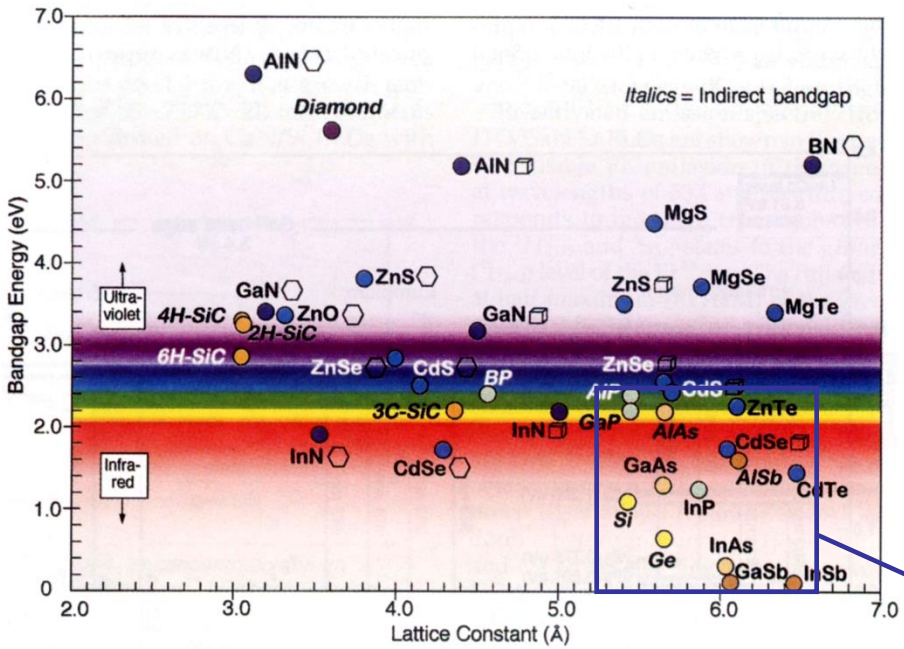


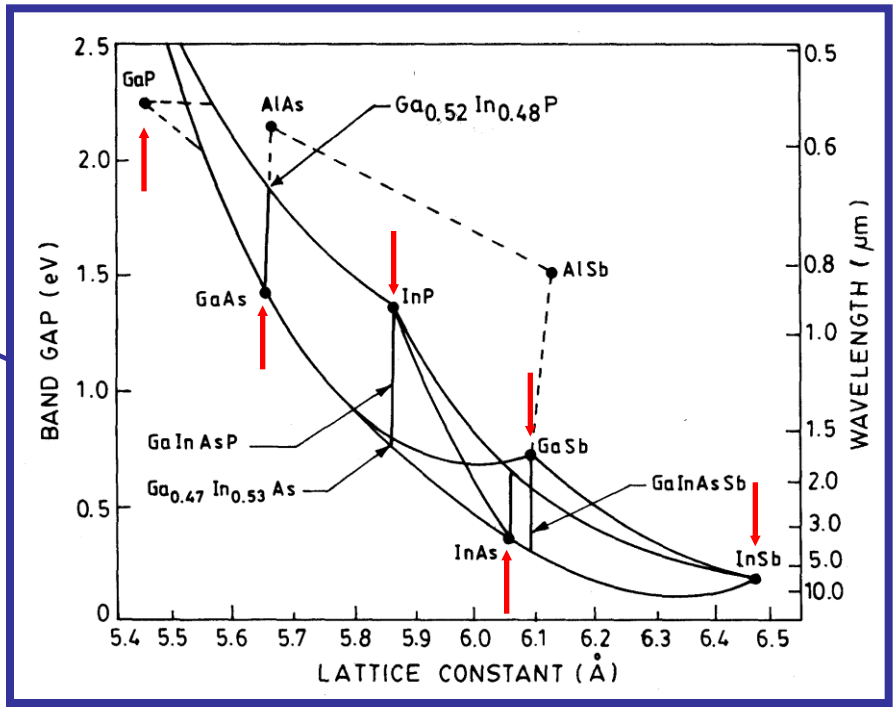
Figure 10. Schematic diagrams of the growth process of GaN on sapphire with an AlN buffer layer.

# Lattice mismatch



advantage of multicomponent systems

$$a = f(\text{composition})$$



**limited number of available substrate crystals!!!**

epitaxy of layers lattice mismatched to the substrate - the most common case

# Lattice mismatch

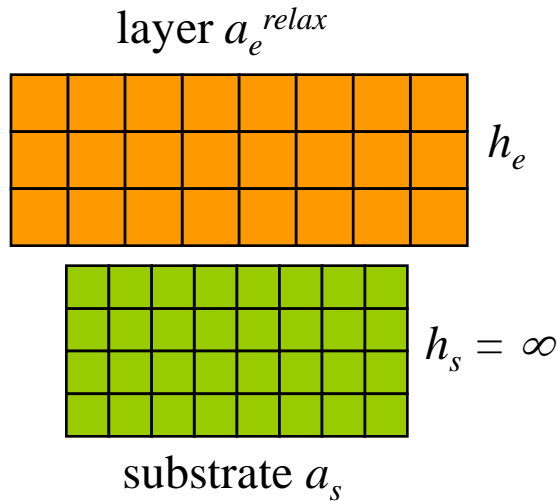
assumptions:

$$h_s = \infty$$

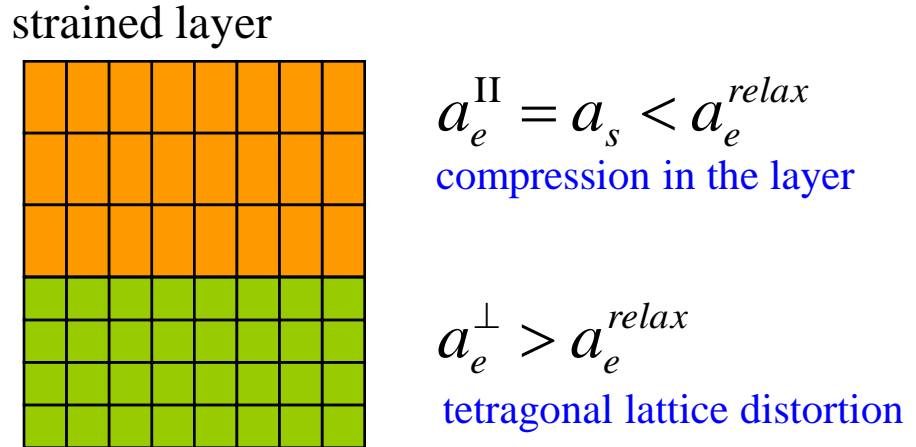
$$h_e < h_{cr}$$

$$a_e^{relax} > a_s$$

before epitaxy



after epitaxy



lattice misfit

$$f = (a_e - a_s) / a_s$$

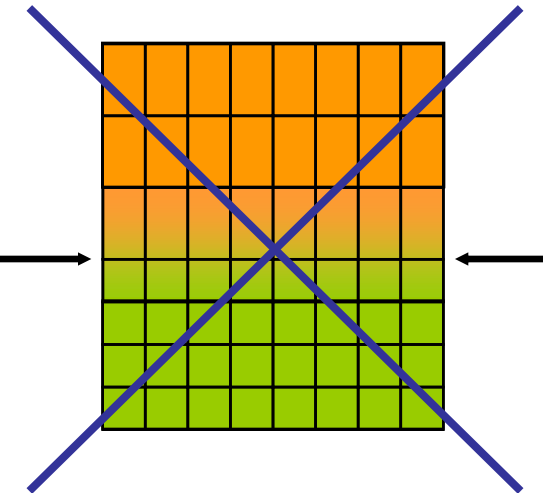
strain energy in the layer

$$E_{el} \propto f^2 \cdot h_e$$



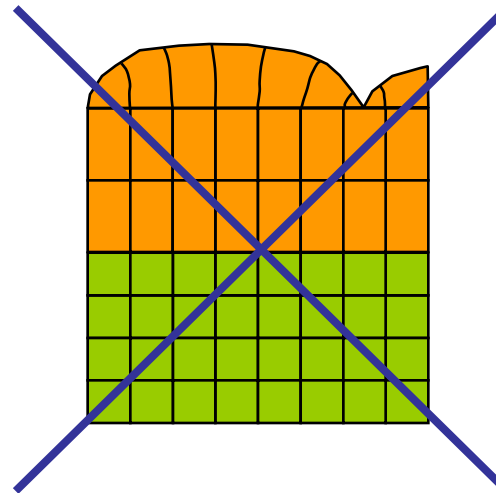
# How to reduce lattice mismatch induced strain energy ?

interdiffusion



- very slow process
- less important in “thick” films
- important in nanostructures

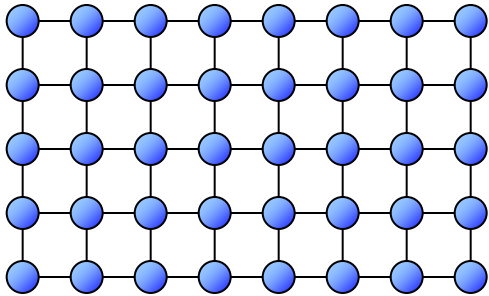
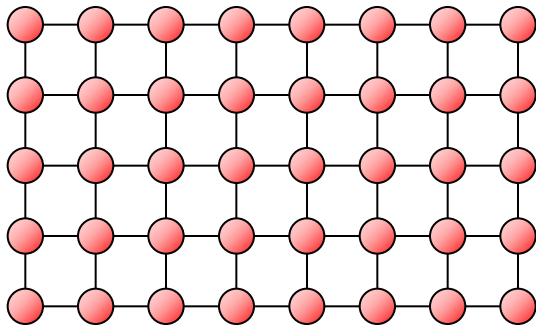
surface deformation



- lattice relaxation at the surface
- important in nanostructures (QDs)
- less important in “thick” films

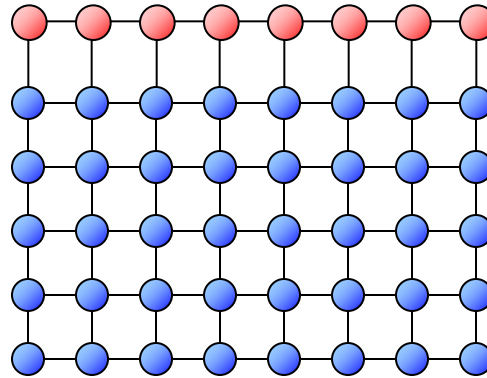
# Generation of misfit dislocations

(misfit dislocations - MD)



separate A and B  $a(B) > a(A)$

$E_e < E_D$  pseudomorphic growth

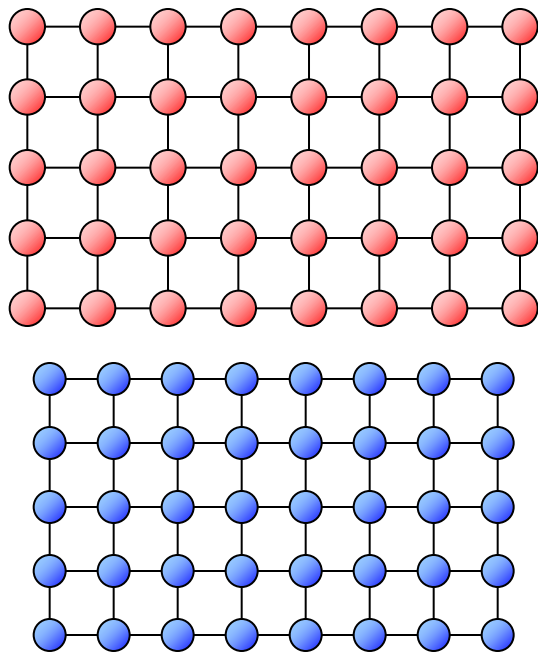


epitaxy of **B** on substrate **A**



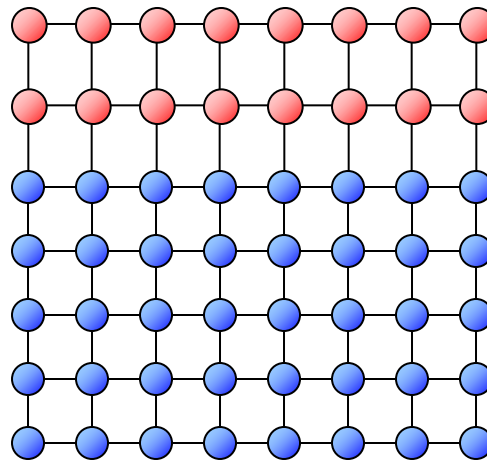
# Generation of misfit dislocations

(misfit dislocations - MD)

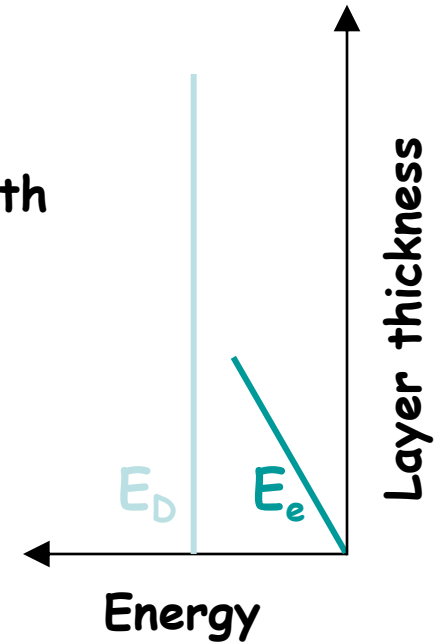


separate A and B  $a(B) > a(A)$

$E_e < E_D$  pseudomorphic growth

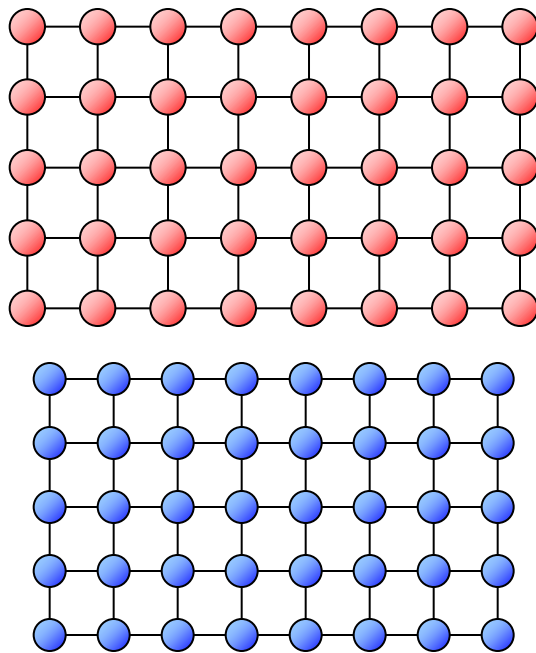


epitaxy of **B** on substrate **A**



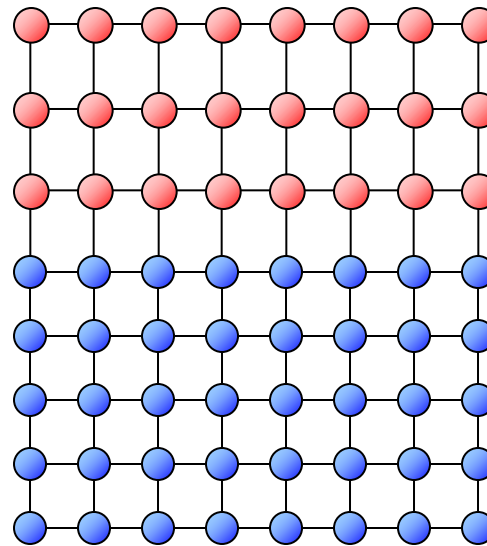
# Generation of misfit dislocations

(misfit dislocations - MD)

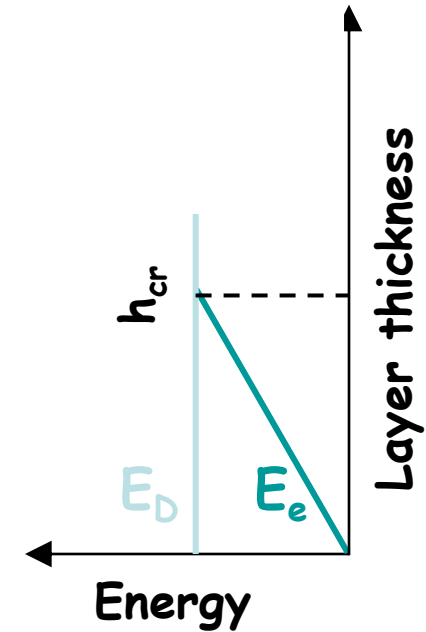


separate A and B  $a(B) > a(A)$

$$E_e = E_D$$



epitaxy of B on substrate A

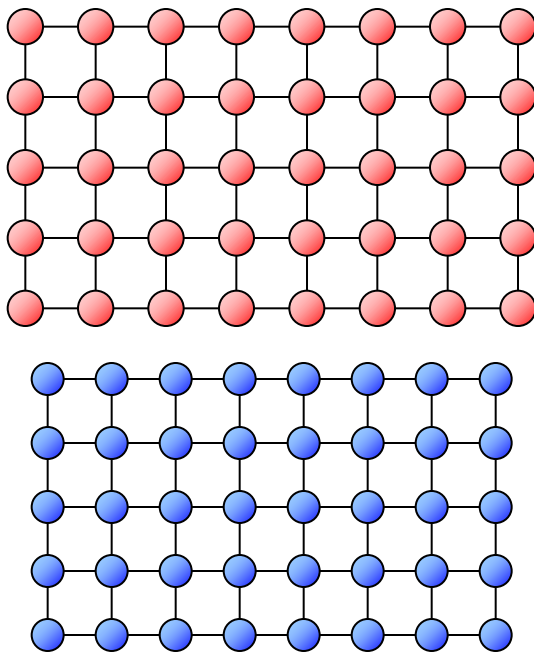


# Generation of misfit dislocations

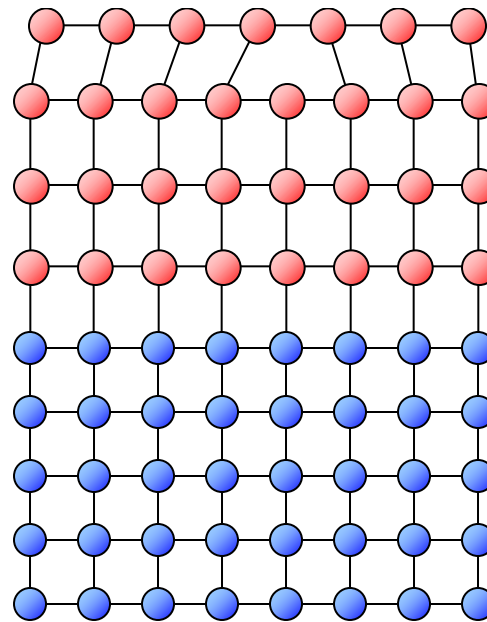
(misfit dislocations - MD)

$$E_e > E_D$$

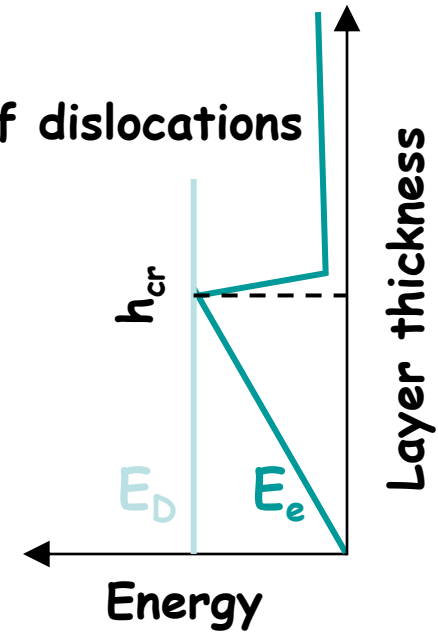
relaxation - generation of dislocations



separate A and B  $a(B) > a(A)$

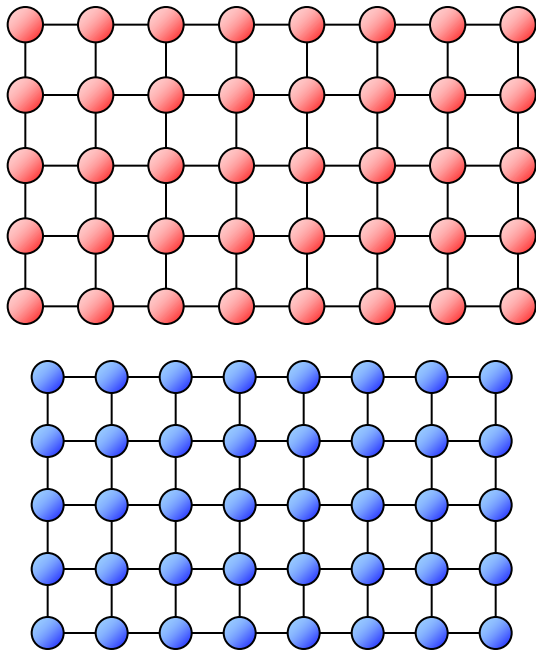


epitaxy of B on substrate A

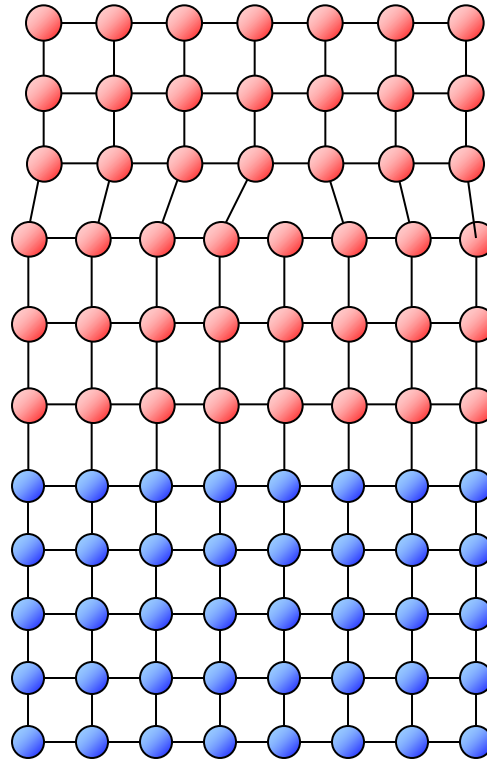


# Generation of misfit dislocations

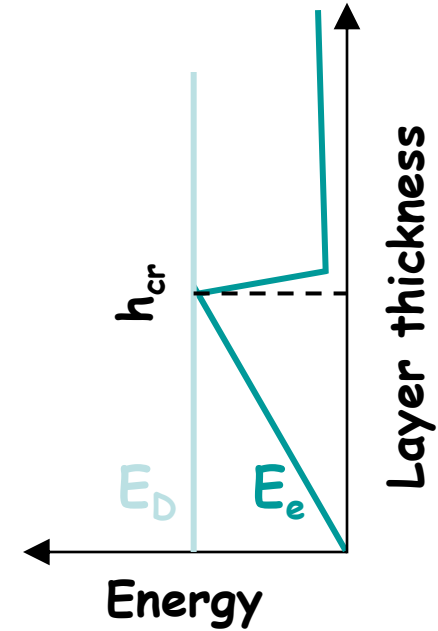
(misfit dislocations - MD)



separate A and B  $a(B) > a(A)$



epitaxy of B on substrate A

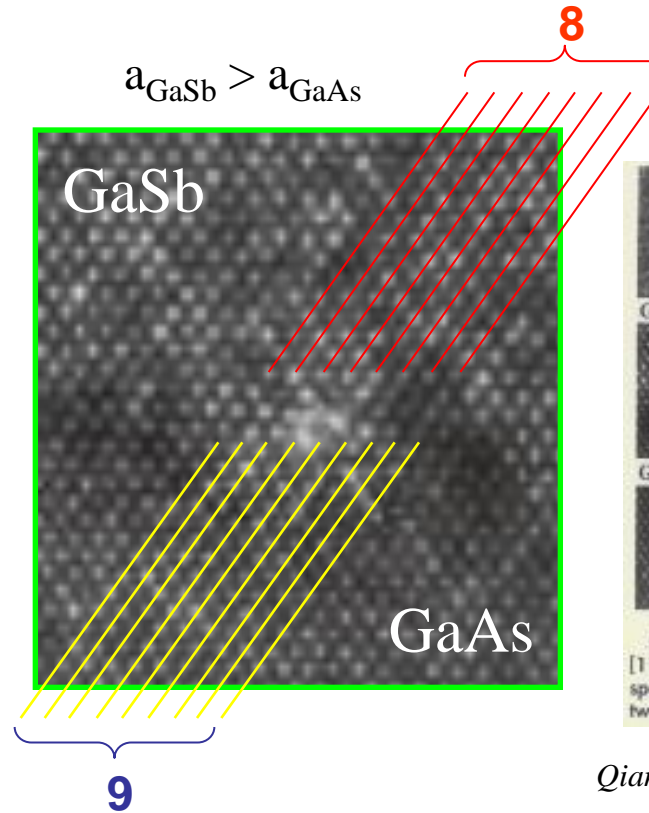
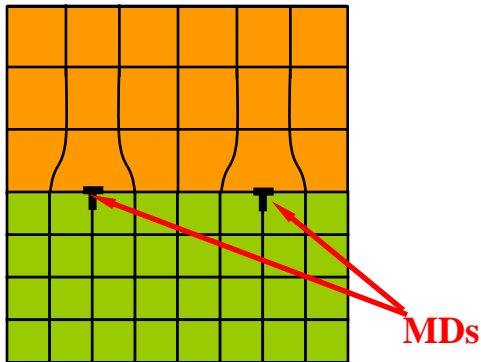


# Generation of misfit dislocations (misfit dislocations - MD)

layer with misfit dislocations

$$h_e > h_{cr}$$

$$a_e^{\parallel} \approx a_e^{\perp} \approx a_e^{relax}$$



Example: GaSb na GaAs

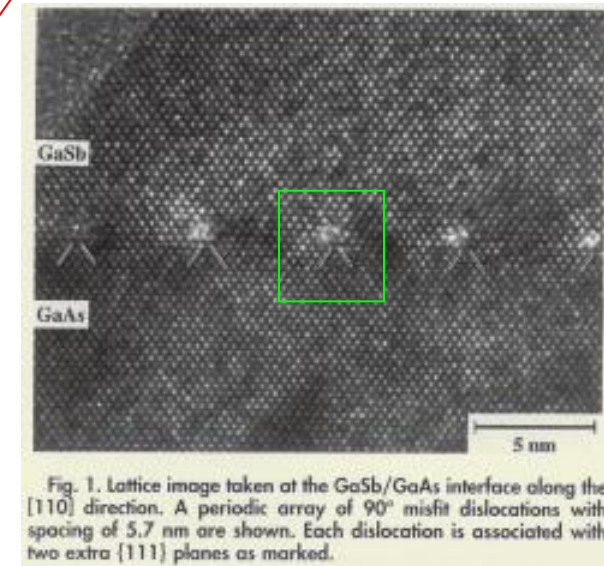


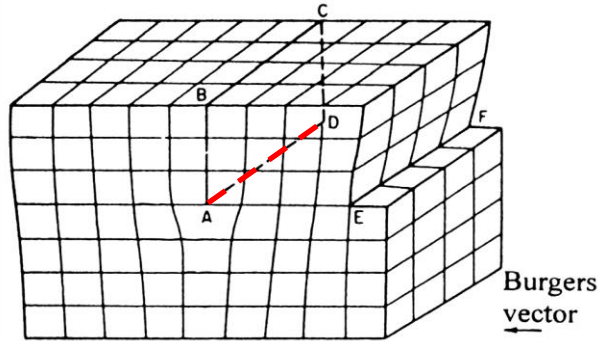
Fig. 1. Lattice image taken at the GaSb/GaAs interface along the [110] direction. A periodic array of 90° misfit dislocations with spacing of 5.7 nm are shown. Each dislocation is associated with two extra {111} planes as marked.

Qian et al. *J. Electrochem. Soc.* **144** (1997) 1430

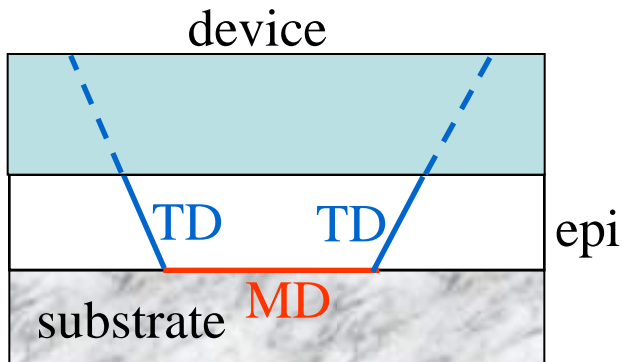
# Do we like misfit dislocations ?

## Threading dislocations

Dislocations cannot terminate inside the perfect crystal



edge dislocations A-D;



MD = misfit dislocation  
TD = threading dislocation

TD dislocations induce nonradiative recombination

Lester et al. *APL* 66 (1995) 1249

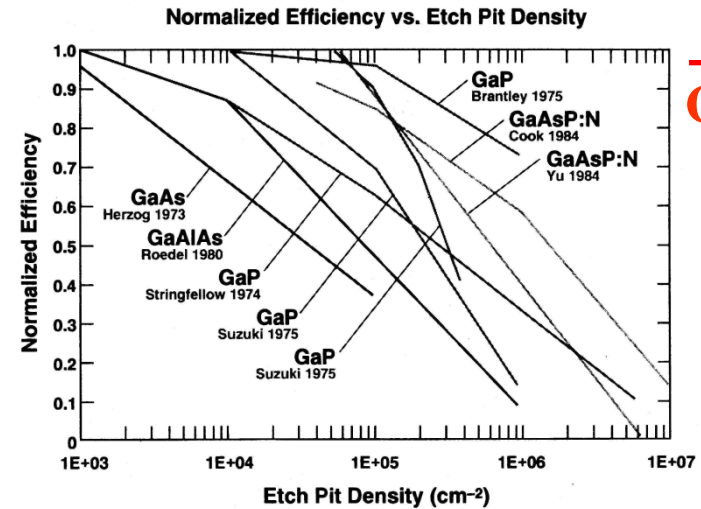


Fig. 3 Dependence of LED efficiency on dislocation density for devices made with a wide range of III-V materials [11].



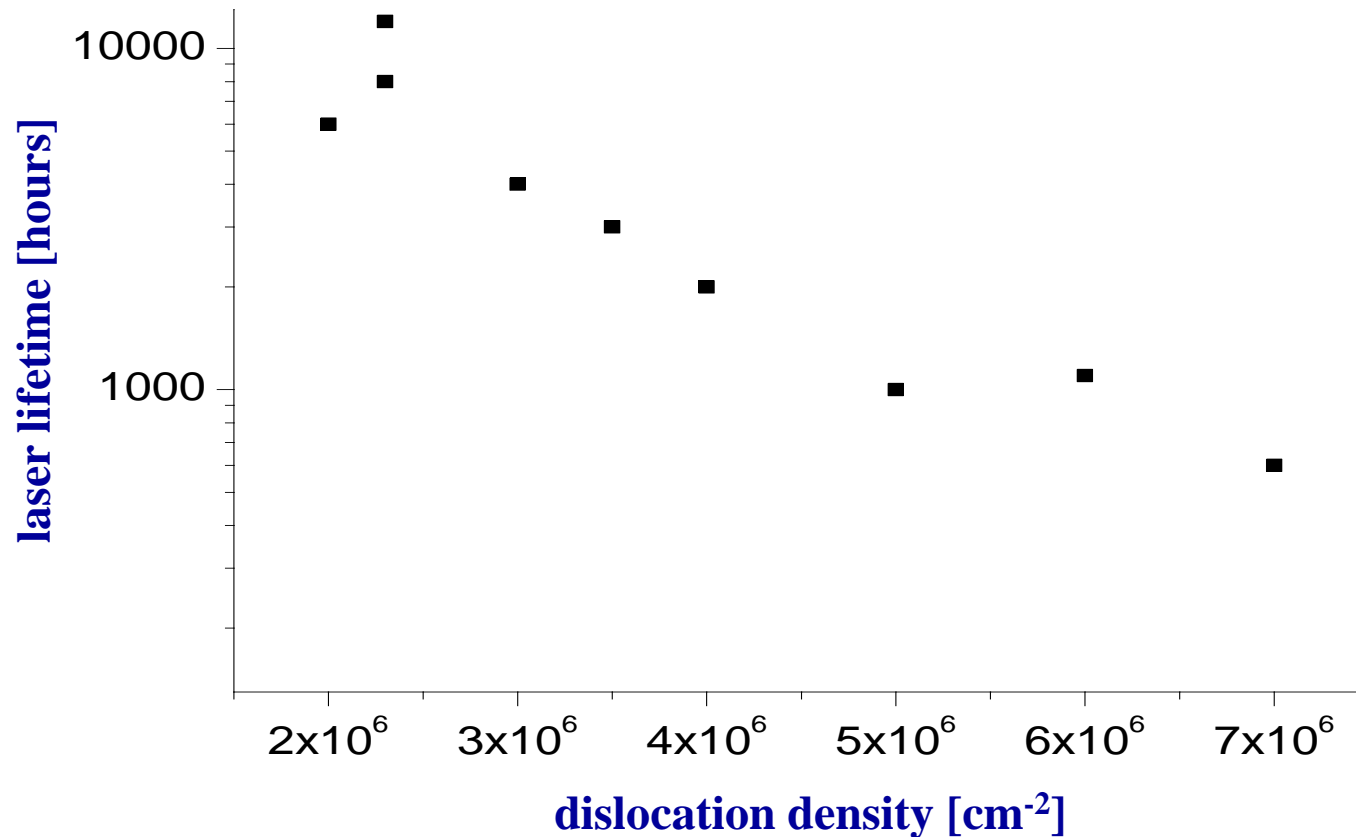
catastrophic degradation



# Do we like misfit dislocations ?

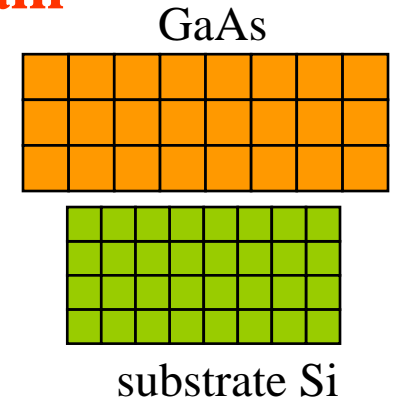
## Threading dislocations

Lifetime of GaN/InGaN laser diodes as a function of dislocation density (from Sony)



# Thermal strain

~~$a_{GaAs} > a_{Si} \Rightarrow$  compressive strain in GaAs grown on Si (???)~~



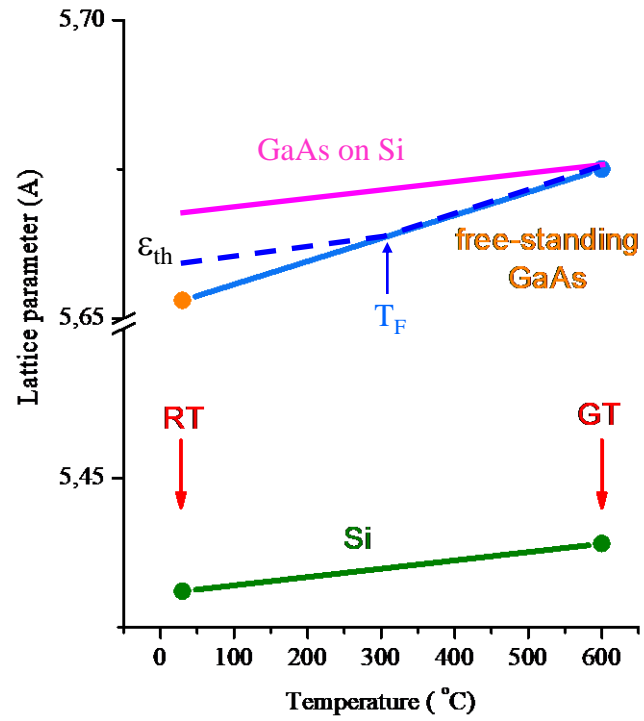
$$\epsilon_{th} = (\alpha_{GaAs} - \alpha_{Si}) \cdot (T_{GT} - T_{RT})$$

tensile strain in GaAs on Si

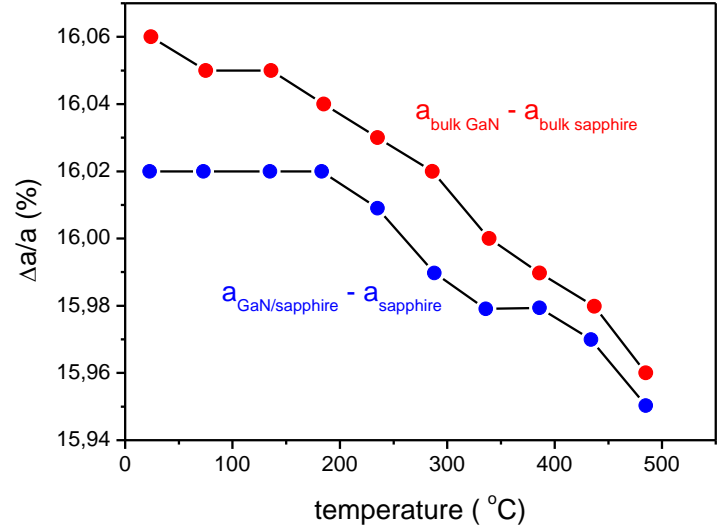
$T_F$

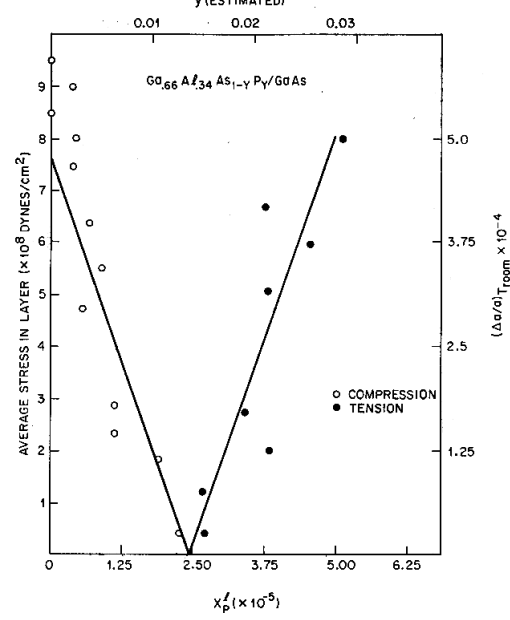
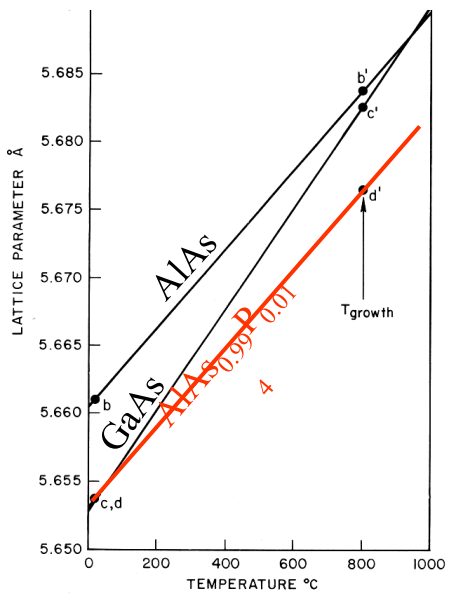
$T_F = 450 \pm 90^\circ C \rightarrow GaAs / Si$   
 $T_F = 250 \pm 100^\circ C \rightarrow InP / Si$   
*Yamamoto & Yamaguchi '88*

residual thermal strain



## GaN/sapphire *Leszczynski et al. JAP '94*

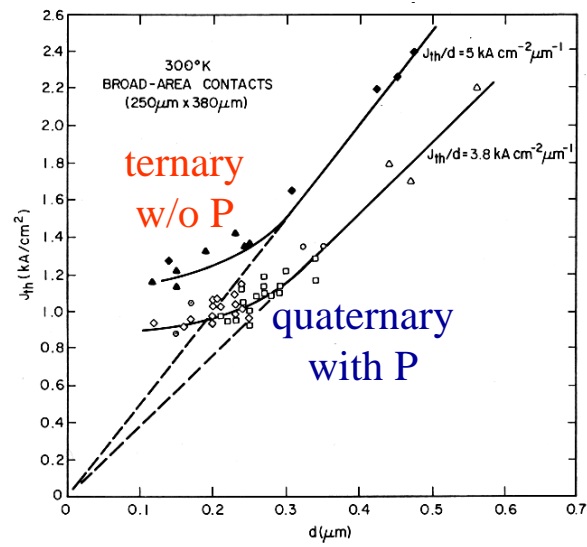
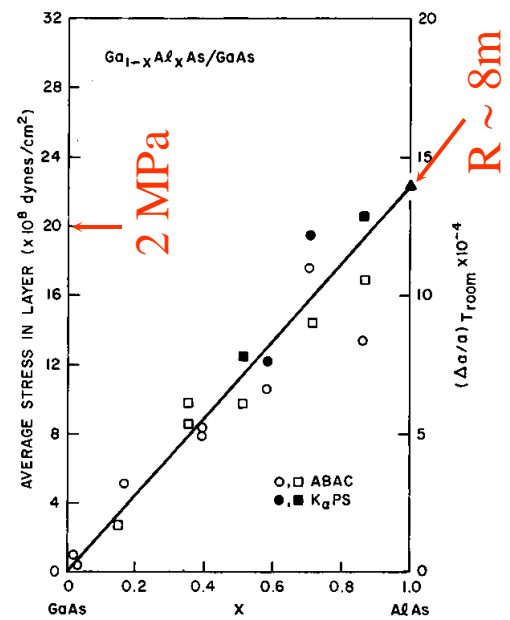




# Thermal strain cont.

- Laser DH GaAlAs/GaAs  
Rozgonyi, Petroff, Panish JCG 27 (1974) 106.

AlGaAs/GaAs -  
considered as an ideal laser system -  
perfect lattice matching



- GaAs on Si -  
cracking of GaAs layers  
thicker than  $\sim 10 \mu\text{m}$   
 $10^9 \text{ dyn/cm}^2 = 100 \text{ MPa}$

Fig. 6. Average film stress versus Al content data determined by ABAC (open circles and squares) and  $K\alpha$ PS (solid circles and squares) techniques. Solid triangle at  $x = 1.0$  is after Ettenberg and Paff<sup>7</sup>).

Fig. 12. Comparison of threshold current density data versus active GaAs layer thickness for lasers with ternary (closed symbols) and quaternary (open symbols) waveguiding layers (see text).

# Lattice mismatch strain - application

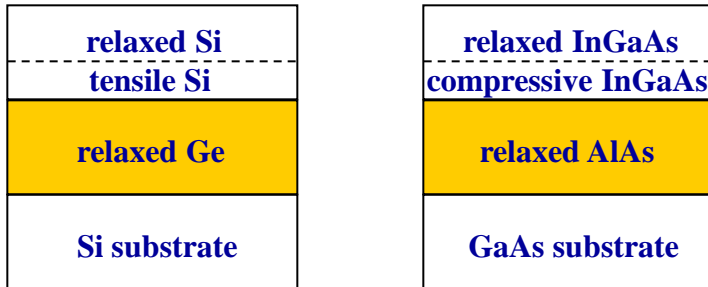
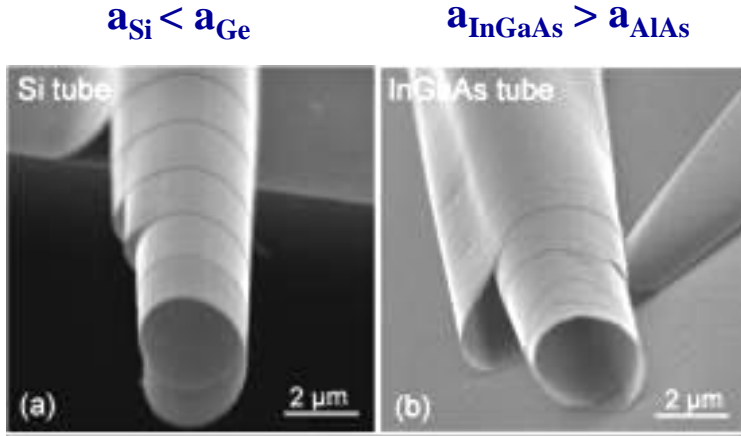
APPLIED PHYSICS LETTERS 89, 223109 (2006)

## Rolled-up micro- and nanotubes from single-material thin films

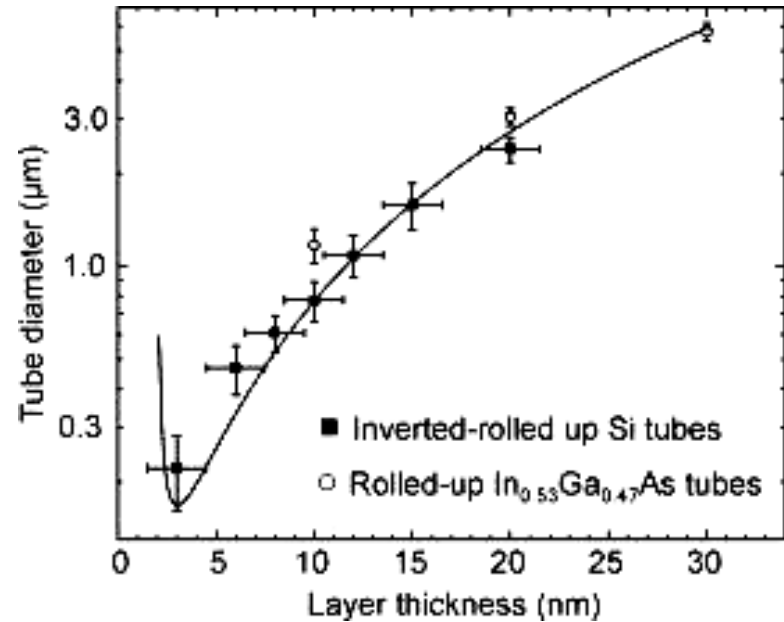
R. Songmuang,<sup>a)</sup> Ch. Deneke, and O. G. Schmidt  
 Max-Planck-Institut für Festkörperforschung, Heisenbergstr. 1, D-70569 Stuttgart, Germany

(Received 1 August 2006; accepted 5 October 2006; published online 28 November 2006)

The authors fabricate well-positioned and size-scalable semiconductor micro- and nanotubes from *single-material* layers. The tubes form when a partially strain-relaxed film, grown at low substrate temperatures, is released from the substrate by selective underetching. The layer rolls *downwards* or *upwards* depending on whether it is initially tensile or compressively strained. They create silicon and indium-gallium-arsenide tubes with diameters accurately tunable by varying the layer thickness. They draw a simple model to describe the mechanism responsible for the tube formation from a single-material thin film. Moreover, the tube diameters are shown to scale with strain and layer thickness. © 2006 American Institute of Physics. [DOI: 10.1063/1.2390647]

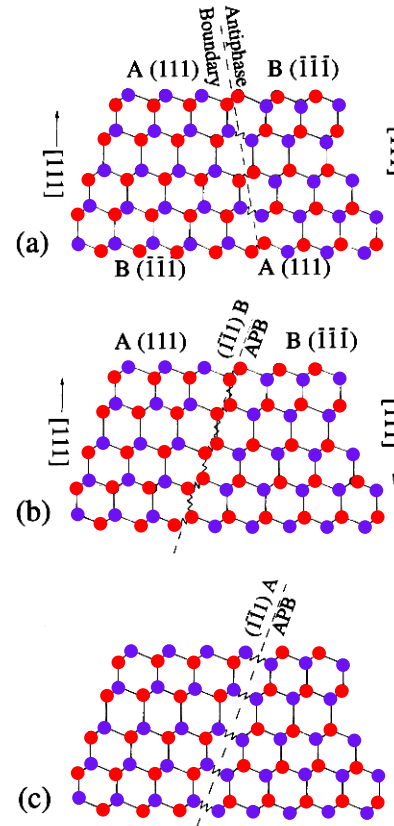
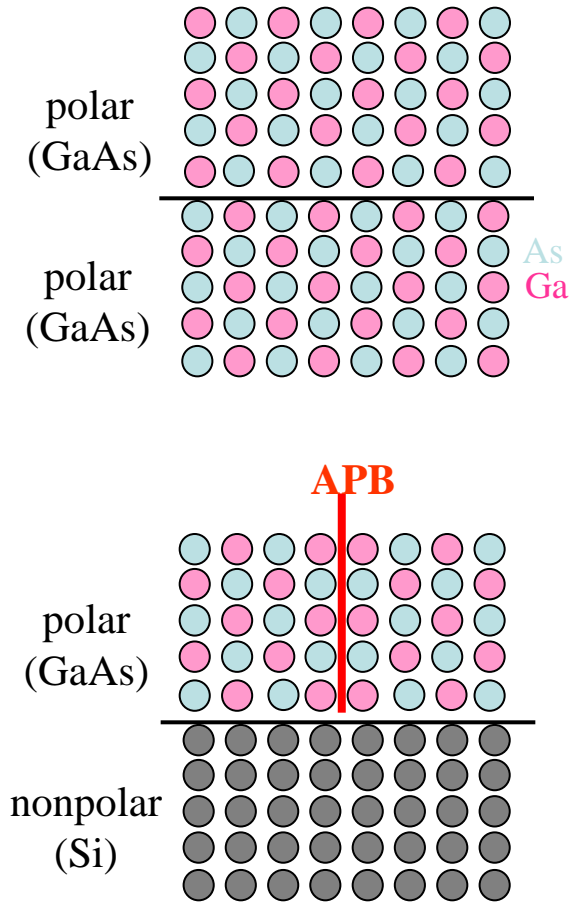


after release by etching



# Antiphase domains (polar on nonpolar)

(antiphase domain boundaries - APB)

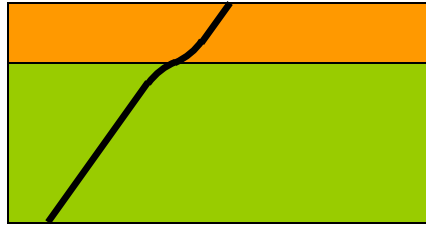


**Fig. 2.11.** Antiphase boundaries in the sphalerite structure [shown in the  $(1\bar{1}0)$  projection]. Zig-zag lines denote wrong bonds. (a) Type I APB on the  $(\bar{1}\bar{1}3)$  plane; (b) type II APB on the  $(\bar{1}\bar{1}1)$  plane involving wrong B-B bonds only and an excess of B atoms; (c) type II APB involving wrong A-A bonds with an excess of A atoms (taken from [2.20])

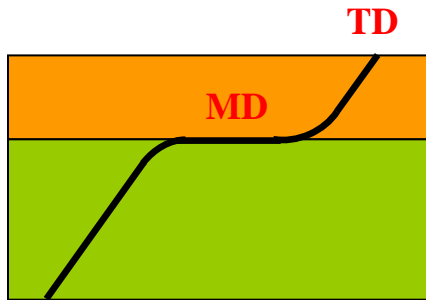
some tricks are needed (e.g. annealing of Si (111) substrate) to reduce density of APB

# Generation of misfit dislocations: the mechanisms

bending of substrate TDs



$h_e \approx h_{cr}$

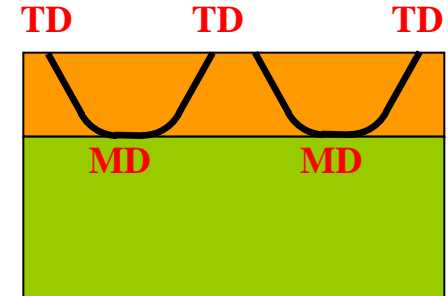
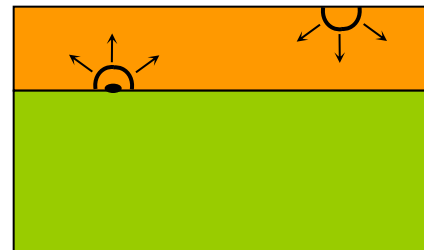


$h_e > h_{cr}$

generation of dislocation half-loops

heterogeneous nucleation

homogeneous nucleation



$$N_{TD} \propto \frac{2}{l_{av}}$$

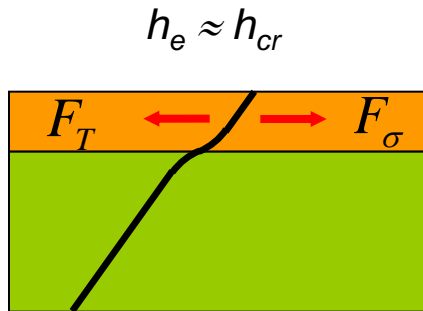
$l_{av}$  - length of MD segment  
 $\text{Ge}_{0.25}\text{Si}_{0.75}/\text{Si } l_{av} \sim 10 \mu\text{m};$

in lattice-mismatched structures

$$\text{EPD} \sim 10^6 - 10^{10} \text{ cm}^{-2}$$

# Critical thickness for MD generation

Matthews & Blakeslee *Journal of Crystal Growth* 27 (1974) 118



misfit stress force

$$F_\sigma \sim b \cdot h_e \cdot f$$

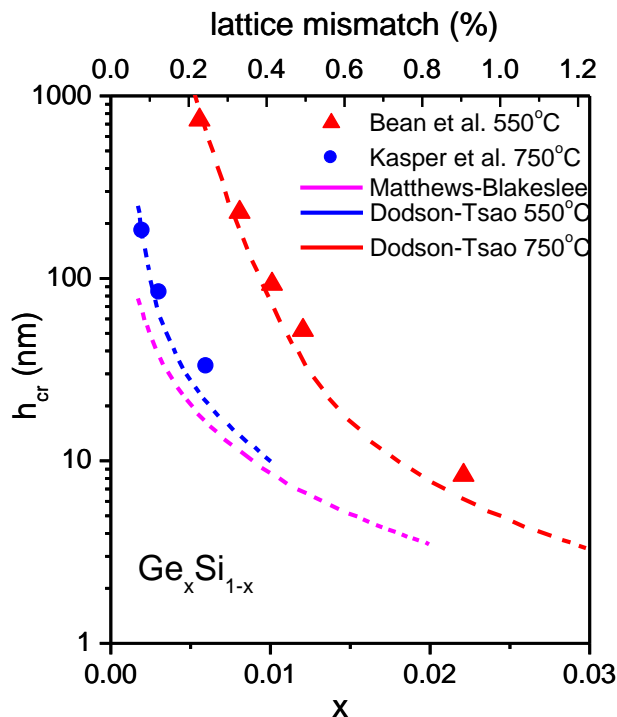
dislocation line tension

$$F_T \sim b^2 \cdot \left[ \ln\left(\frac{h_e}{b}\right) + 1 \right]$$

$F_\sigma > F_T \longrightarrow$  growth of MD segment

$F_\sigma = F_T \longrightarrow h_e = h_{cr}$  (onset of MD generation)

**equilibrium model**



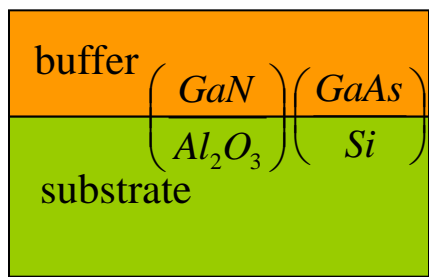
**Dodson & Tsao** *APL* 51 (1987) 1325; 52 (1988) 852

velocity of MD  $\propto$  excess stress (actual stress - stress @ EQ)

strain = f( $h_e$ , T, t, ...)

**dynamical model**

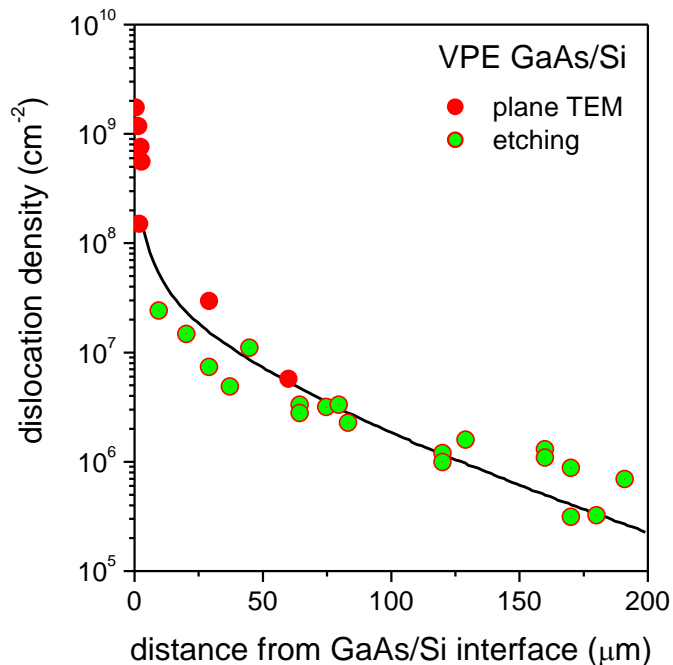
# Buffer layers



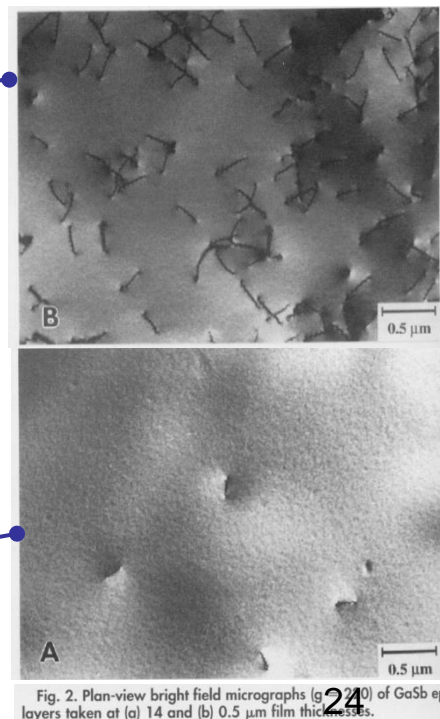
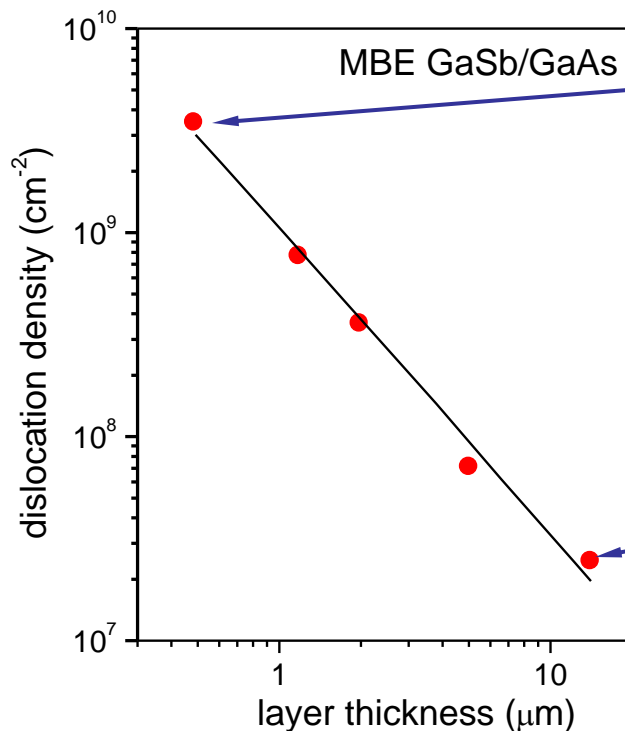
**buffer** = fully (?) relaxed epitaxial layer with required value of the lattice parameter grown on available substrate wafer

new substrate for next epitaxial growths

Tachikawa & Yamaguchi APL 56 (1990) 484



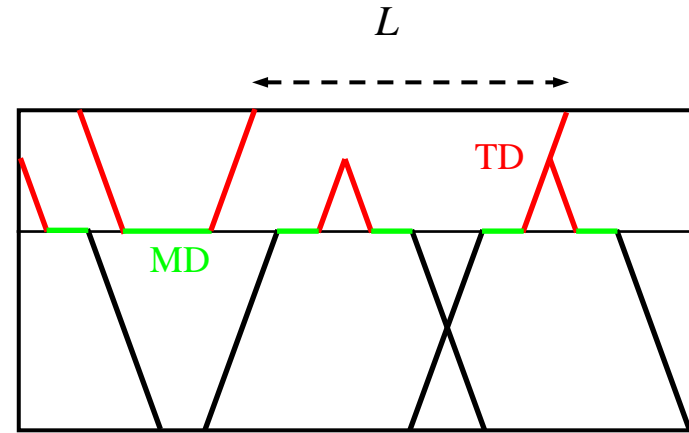
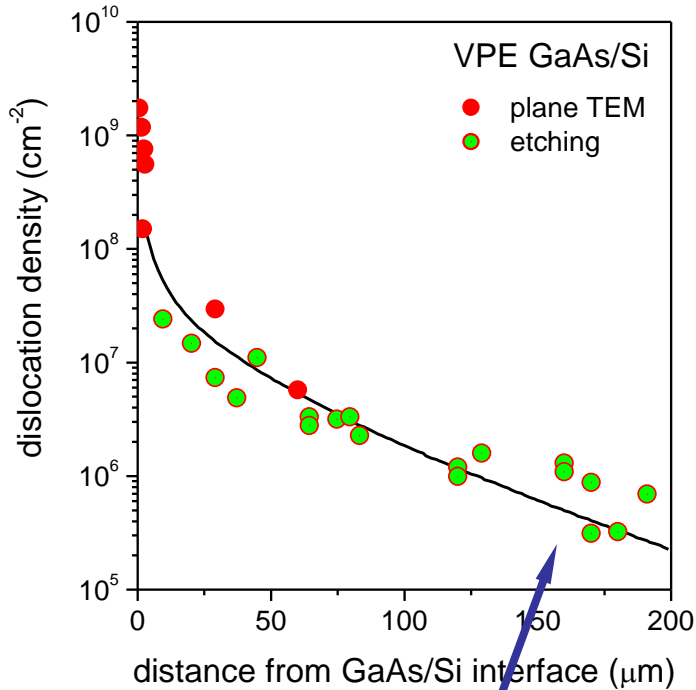
Qian et al. J. Electrochem. Soc. 144 (1997) 1430





# Threading dislocations in thick buffers

Tachikawa & Yamaguchi *APL* 56 (1990) 484



$$L = 1/\sqrt{N_{TD}}$$

$$N_{TD} = 10^{10} \text{ cm}^{-2} \Rightarrow L = 100 \text{ nm}$$

reactions of dislocations highly efficient

$$N_{TD} = 10^6 \text{ cm}^{-2} \Rightarrow L = 10 \mu\text{m}$$

low efficiency of dislocation reactions

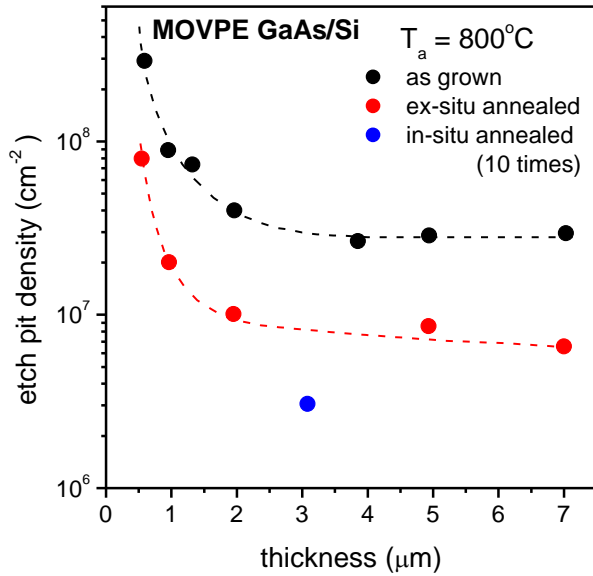
Why this plot saturates for thicker films ?

How to speed up reduction of EPD with buffer thickness?

# Annealing

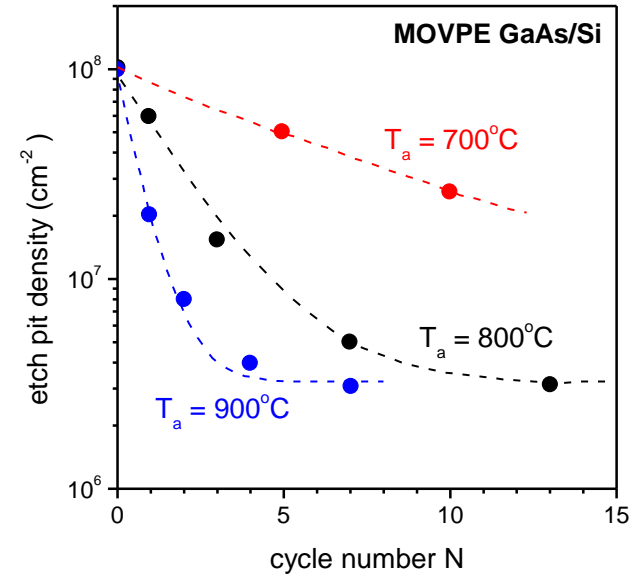
thermal strain  $\leftrightarrow$  driving force for TD movement

Yamamoto & Yamaguchi MRS 116 (1988) 285



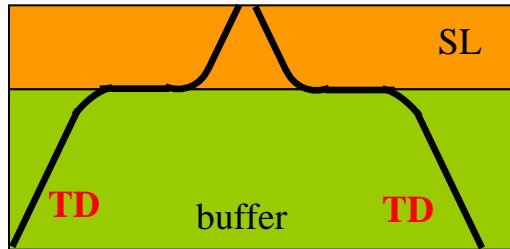
- annealing *in-situ*:
  - growth 1  $\mu\text{m}$  GaAs
  - annealing ( $T_{\text{gr}} \rightarrow \text{RT} \rightarrow T_a$ )  $\times N$
  - growth 2  $\mu\text{m}$  GaAs @  $T_{\text{gr}}$

Yamaguchi et al. APL 53 (1988) 2293



# Filtration of TDs by strained superlattice

lattice mismatch strain  $\leftrightarrow$  driving force of bending and movement of dislocations



Qian et al. *J. Electrochem. Soc.* 144 (1997) 1430

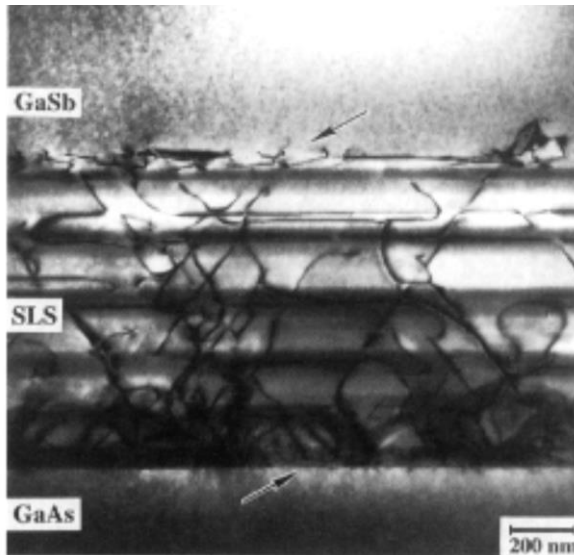
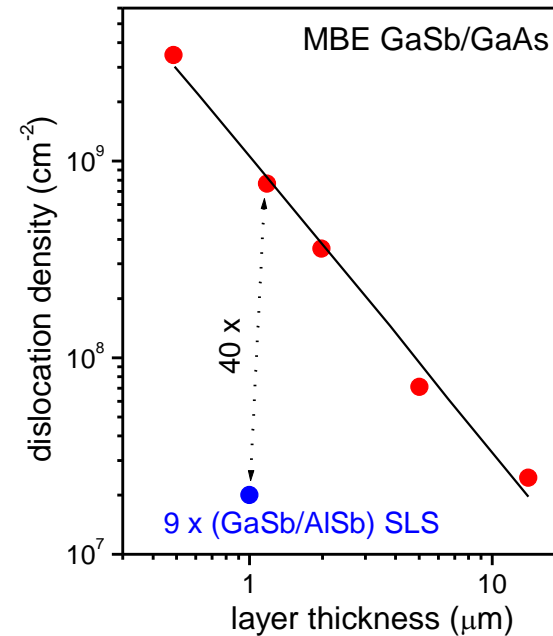


Fig. 5. Cross-sectional bright field micrograph shows the dislocation filtering of the GaSb/AlSb SLS. The majority of threading dislocations are bent by the SLS resulting in low defect density at the top GaSb layer.

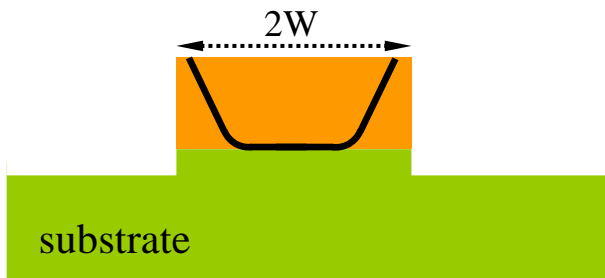


- SLS filter efficient for high TD densities
- careful growth needed (no new defects)
- sometimes annealing used in addition

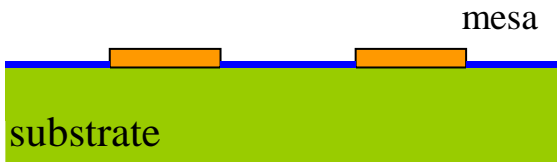
TD density  $< 10^6 - 10^7 \text{ cm}^{-2}$   
not achievable in homogeneous buffers

# Epitaxy on „small” substrates

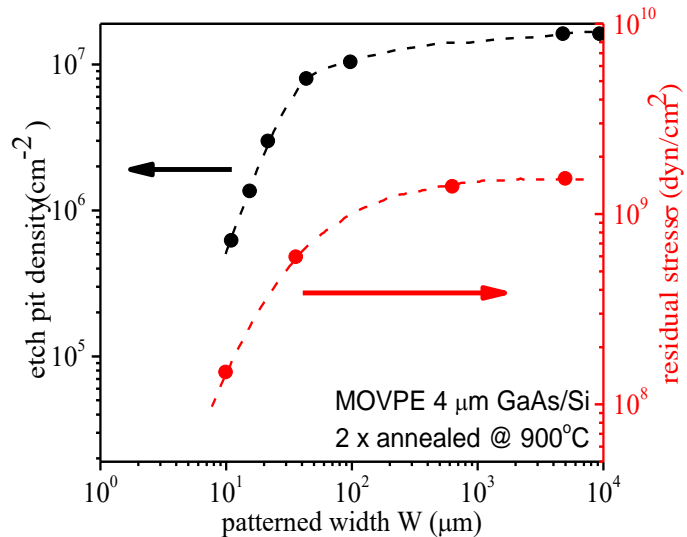
dislocations terminate at the sidewalls



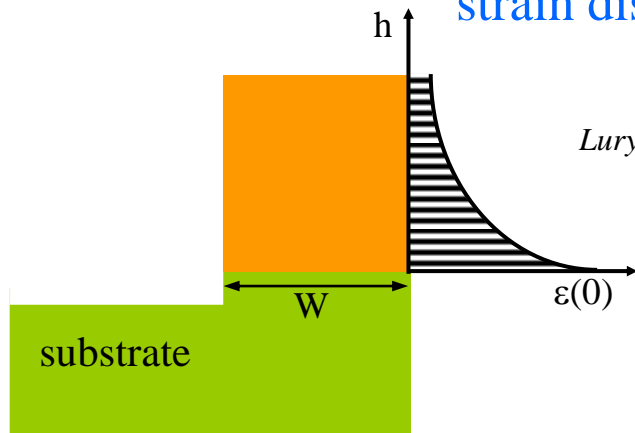
Selective Area Growth (SAG)  
on masked substrate



Yamaguchi et al. APL 56 (1990) 27



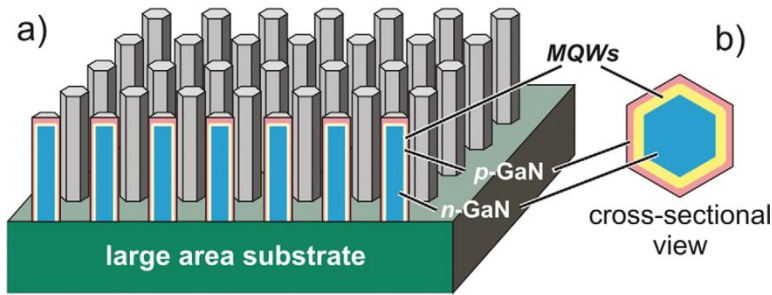
strain distribution in mesa



Luryj & Suhir APL 49 (1986) 140

$$E_{strain}(h, W) \leftrightarrow E_{dislocation} \rightarrow h_{cr} \text{ decreases with } W$$

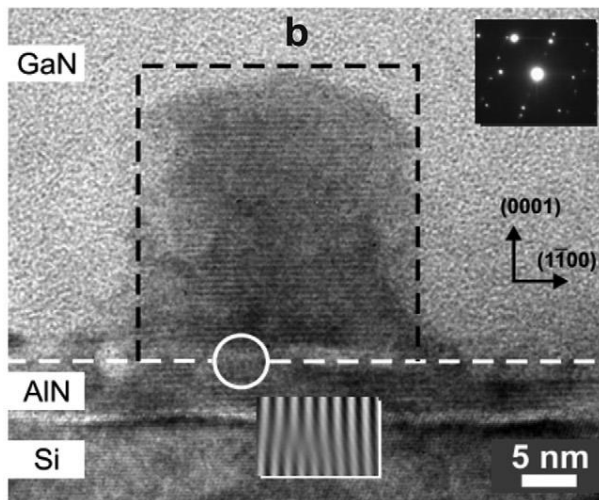
# Epitaxy on „small” substrates - Nanowires (NWs)



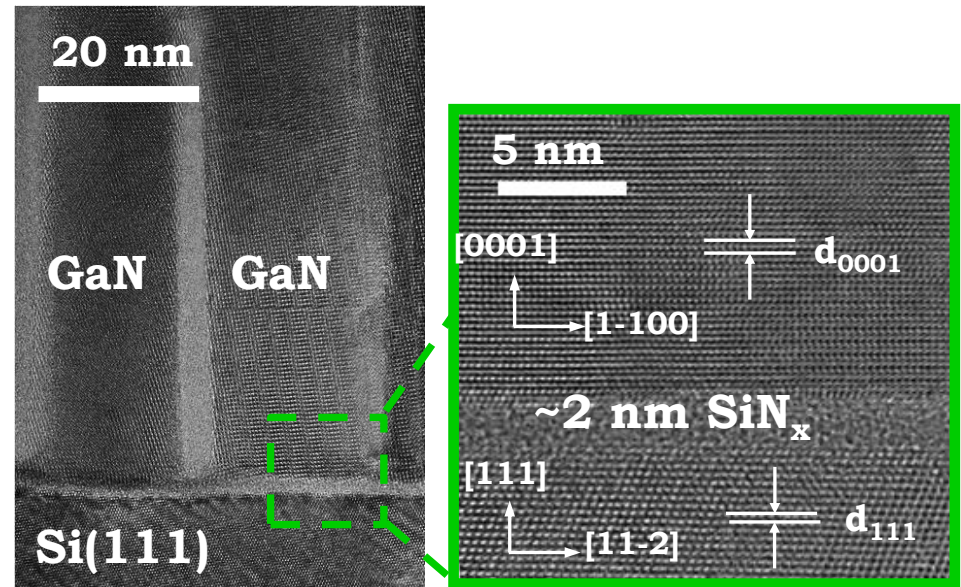
small NW footprint  
(small contact area with the substrate)

## GaN NWs on nitrated Si

### GaN NWs on AlN/Si



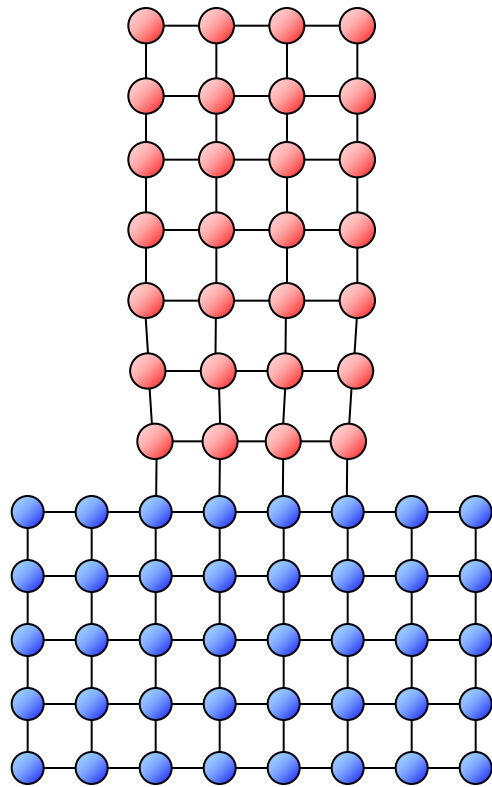
Consonni et al. PRB 81 (2010) 085310



A. Wierzbicka, et al. Nanotechnology 24 (2013) 035703

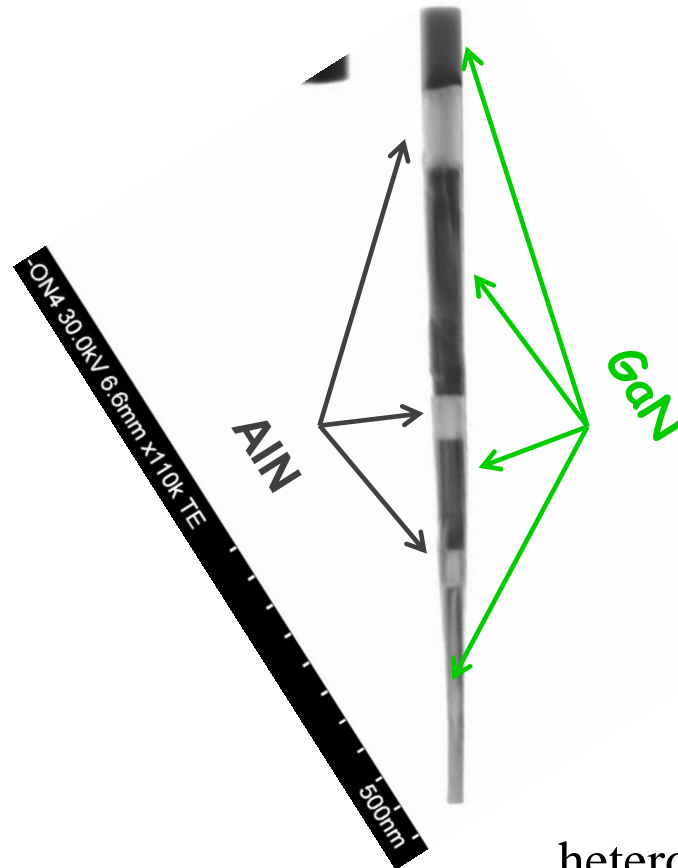
perfect structural quality of NWs despite their large lattice mismatch with the substrate

# Epitaxy on „small” substrates - Nanowires (NWs)



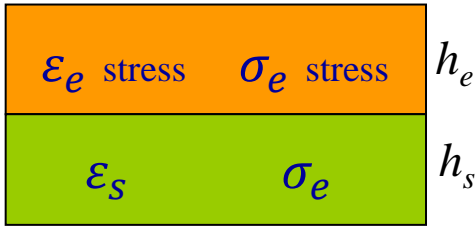
nanowire A on substrate B

$$a(B) > a(A)$$



in NW geometry  
heterostructures with quality  
not available in planar form  
can be fabricated

# Growth on „thin” substrates – concept of compliant substrates



Y.H. Lo, APL 59 (1991) 2311

$$\frac{1}{h_{cr}} = \frac{1}{h_{cr}^\infty} - \frac{1}{h_s}$$

$h_{cr}$  critical thickness

$$h_{cr}^\infty = h_{cr}(h_s = \infty)$$

for  $h_s > h_{cr}^\infty$

equal forces in both parts

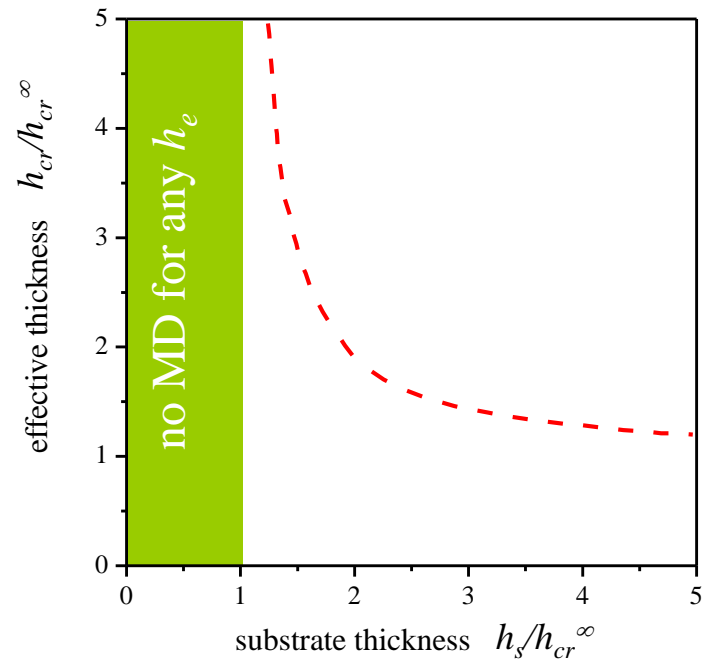
$$\sigma_e \times h_e = \sigma_s \times h_s$$

Hook's law

$$\sigma \propto \epsilon$$

$$\epsilon_0 = \epsilon_e + \epsilon_s = \frac{\Delta a}{a}$$

$$\frac{\epsilon_e}{\epsilon_0} = \frac{h_s}{h_e + h_s} \quad h_s = h_e \Leftrightarrow \epsilon_e = \epsilon_s$$

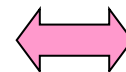


partial transfer of strain from epi to substrate



larger critical thickness

$$h_s < h_{cr}^\infty \Rightarrow h_{cr} = \infty$$



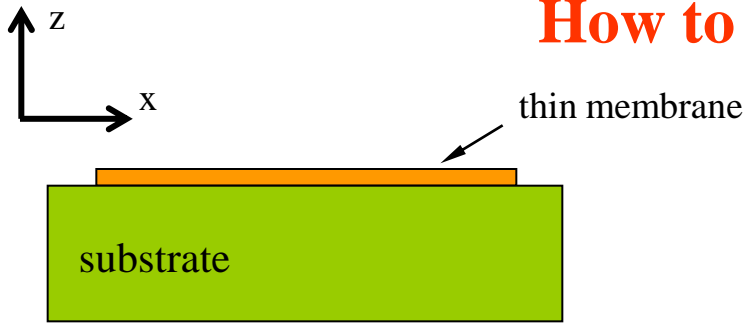
substrate

layer

layer

substrate

# How to produce thin substrate membranes?



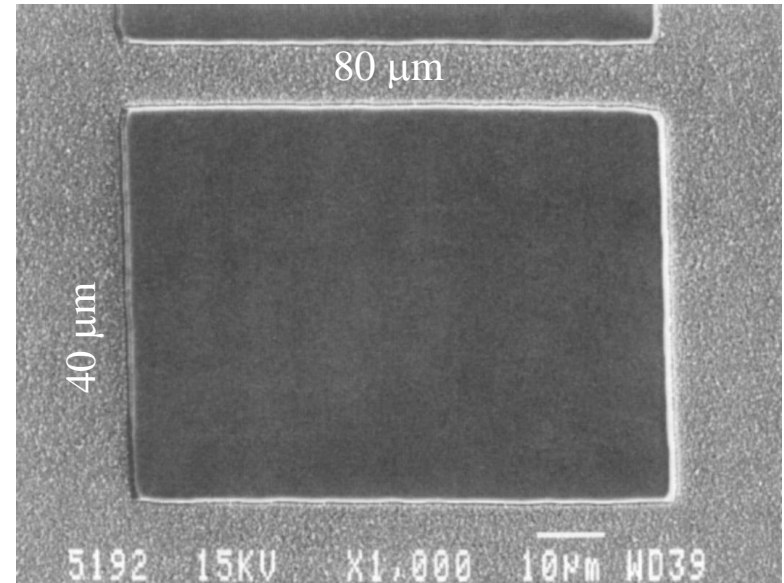
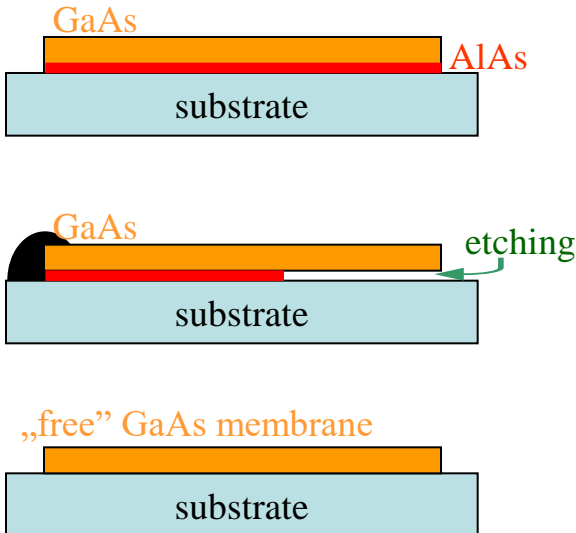
*De Boeck et al. JJAP 30 (1991) L423*

MBE 1.3  $\mu\text{m}$  GaAs/Si;  
 patterning + mesa release & deposition  
 MBE growth of 1  $\mu\text{m}$  GaAs

## Requirements:

- strong bonding with the substrate in the z direction
  - to avoid rolling up of the membrane
- weak bonding with the substrate in the x direction
  - sliding of the membrane on the substrate possible
- large area and small thickness of the membrane

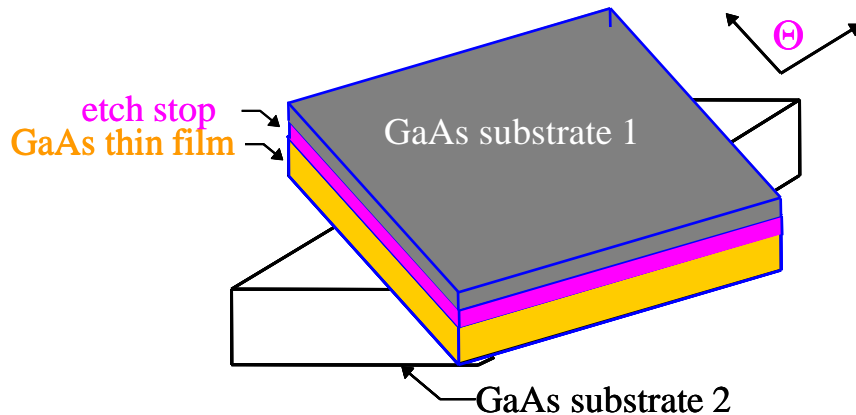
## patterning + mesa release & deposition



PL: no strain in GaAs grown on the membrane  
 large strain in GaAs grown on bulk Si



# Formation of thin substrates by wafer bonding



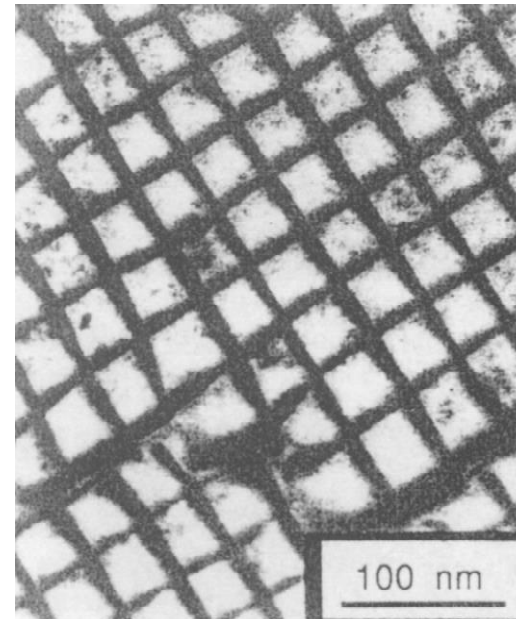
- connection:  $T \sim 550^\circ\text{C}$  in  $\text{H}_2$  or UHV
- pressure:  $\sim 200\text{ g/2 inch wafer}$
- etching to remove the host substrate
- twist angle  $\Theta$ :  $0 - 45^\circ$
- very thin layers (10 ML) can be bonded

## Problems:

- gas bubbles at the joint leading to cracks
- residual contaminations at the joint
- problems with cleaving
- difficult technology

## Twist-bonded interface

*Benemara et al. Mat. Sci. Eng.B 42 (1996) 164*



Plane-view TEM  
of bonded Si wafers  
( $\Theta \sim 0.6^\circ$ )

dense network of screw dislocations



**“soft” connection**

distance between dislocations =  $f(\Theta)$   
no threading dislocations

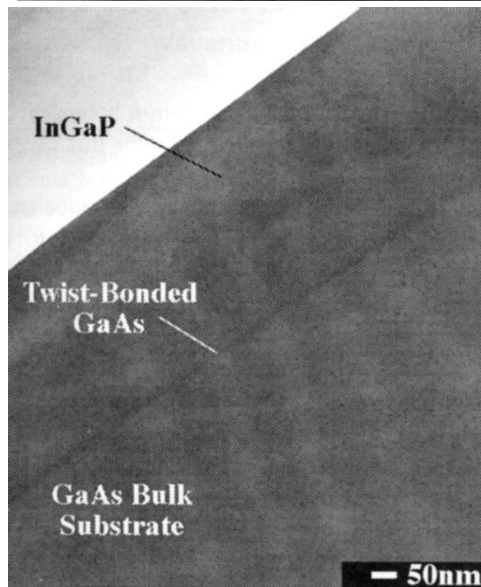
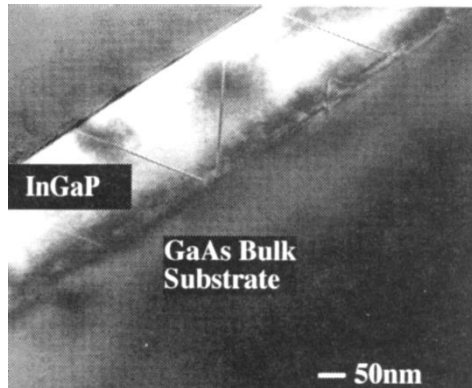
# Universal compliant substrate

*Ejeckam et al. APL 70 (1997) 1685*

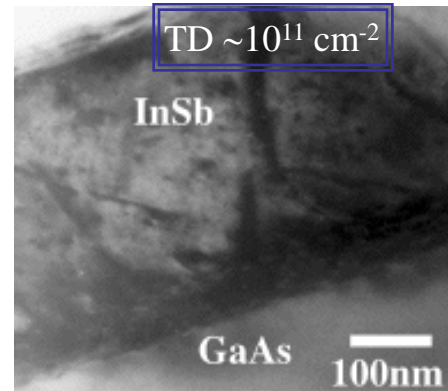
film GaAs 10 nm;  $\Theta \sim 17^\circ$  in  $H_2$

300 nm of InGaP on GaAs by MOVPE

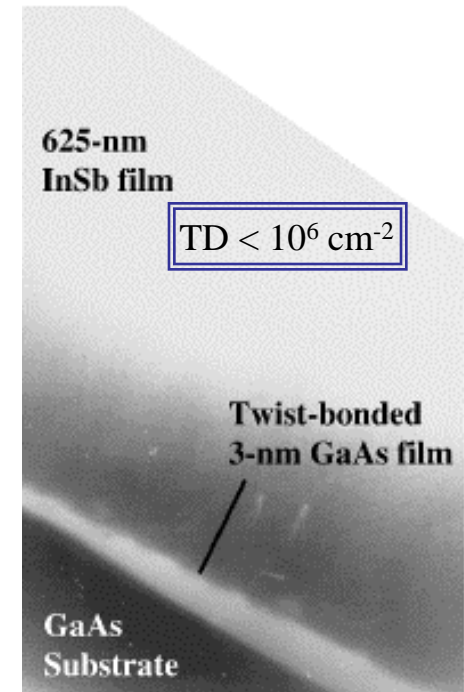
$f = 1\% \Rightarrow h_e = 30 \times h_{cr}^\infty$  (10 nm)



*Lo et al. Cornell Sci. News 1997;*  
*Ejeckam et al. APL 71 (1997) 776*



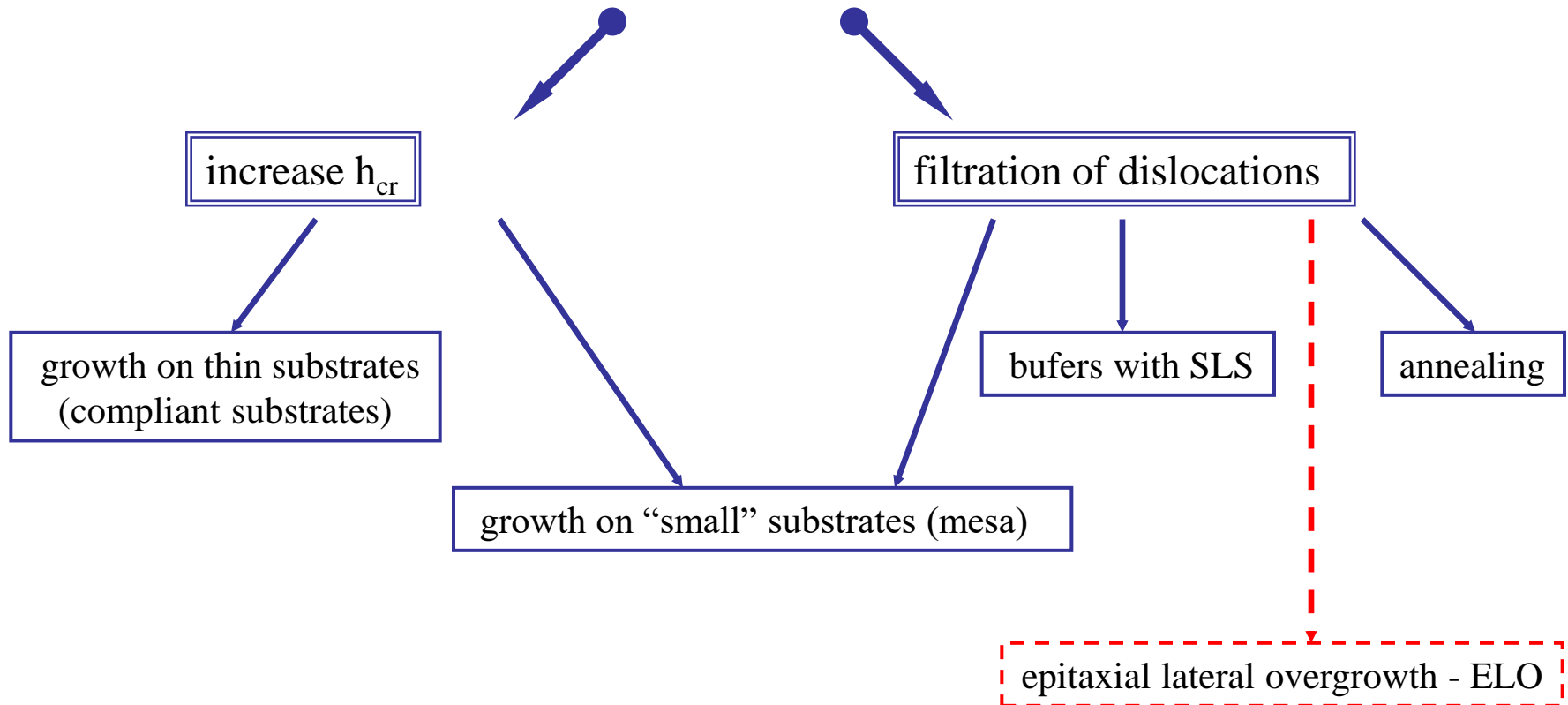
InSb on GaAs  $f = 14.7\%$



## Conclusion:

- spectacular laboratory results;
- nice confirmation of the effect of strain transfer from epilayer to the thin substrate
- difficult technology
- no reports on a wide application in the industry

# Methods to reduce defect density in lattice mismatched epitaxial structures - summary



**There are no universal method to reduce dislocation density in lattice mismatched heterostructures;**

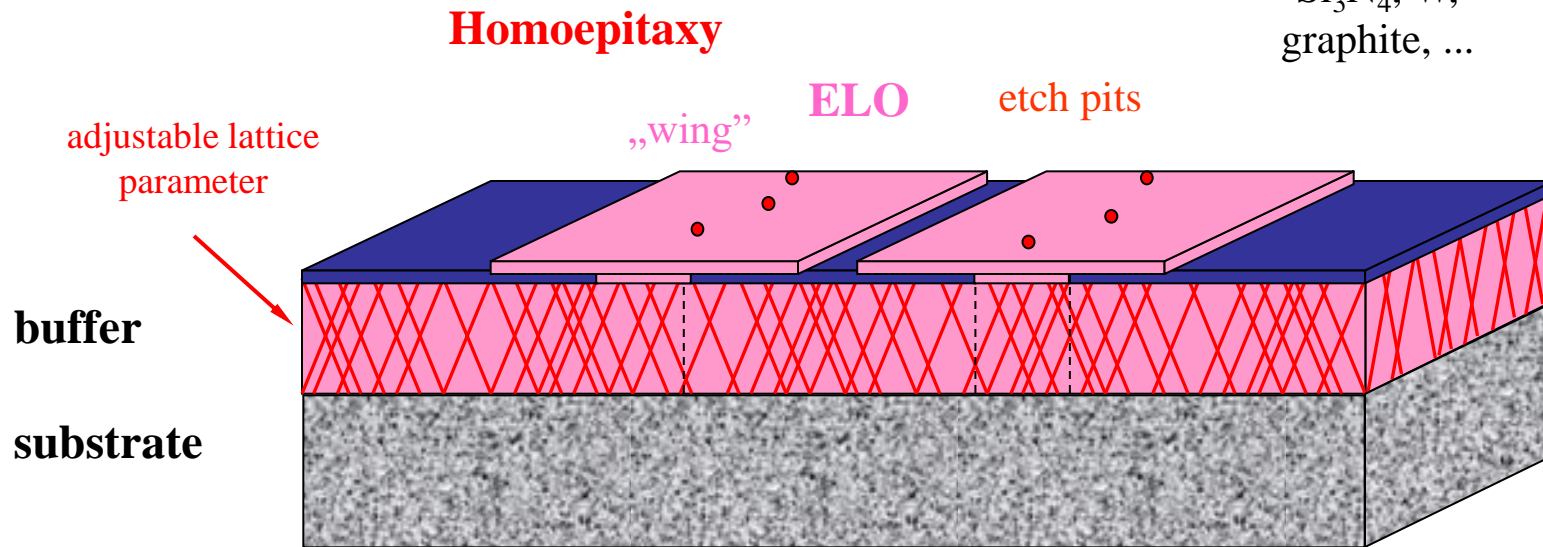
**The best way is to avoid lattice mismatch – find the suitable substrate !!!**

# Epitaxial Lateral Overgrowth - ELO

*How to grow low EPD homoepitaxial layers on heavily dislocated substrates ?*

⇒ **ELO**

**mask:** SiO<sub>2</sub>,  
Si<sub>3</sub>N<sub>4</sub>, W,  
graphite, ...



MOVPE GaN: S = 5 – 20 μm; W = 2 - 5 μm  
LPE GaAs: S = 100 – 500 μm; W = 6 - 10 μm